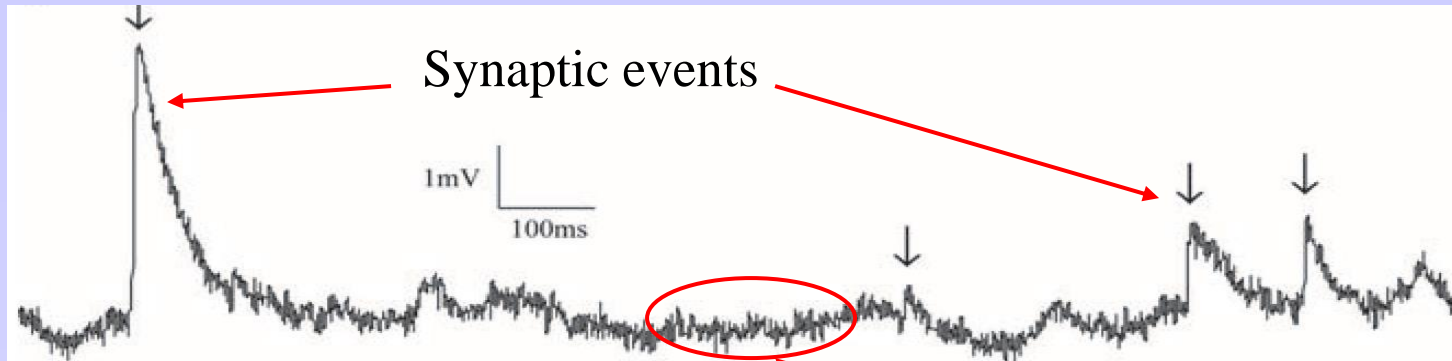


## Unit 3

# Spontaneous Activity

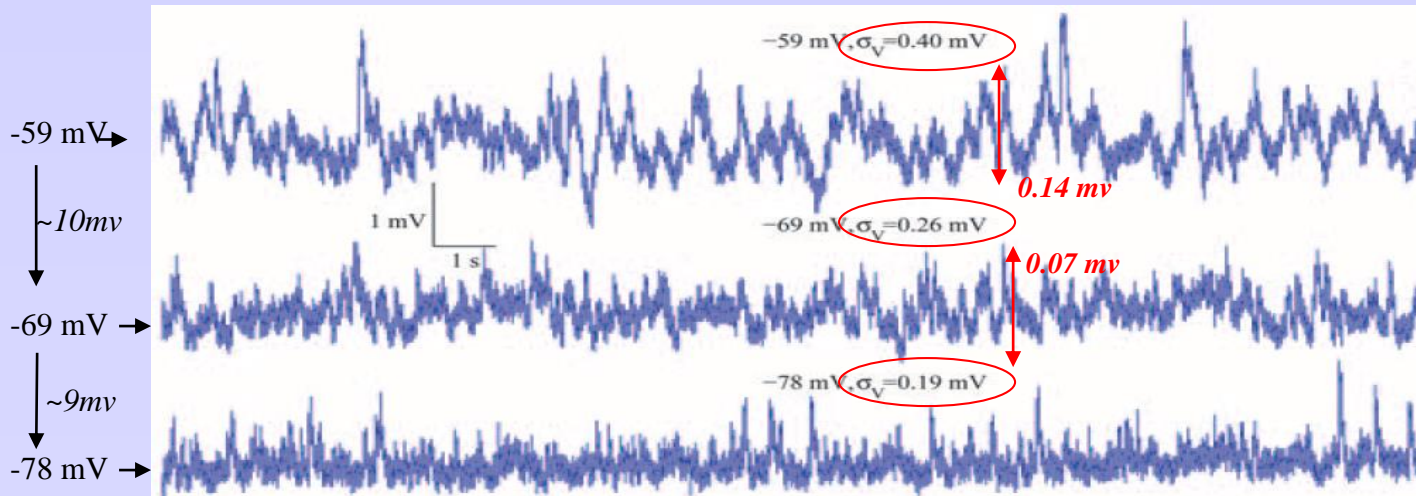
# Spontaneous Activity

- Definition: Spiking activity that is not (temporally) related to a stimulus.
- E.g. Subthreshold 'noise':



(Jacobson et. al. 2005)

Membrane noise



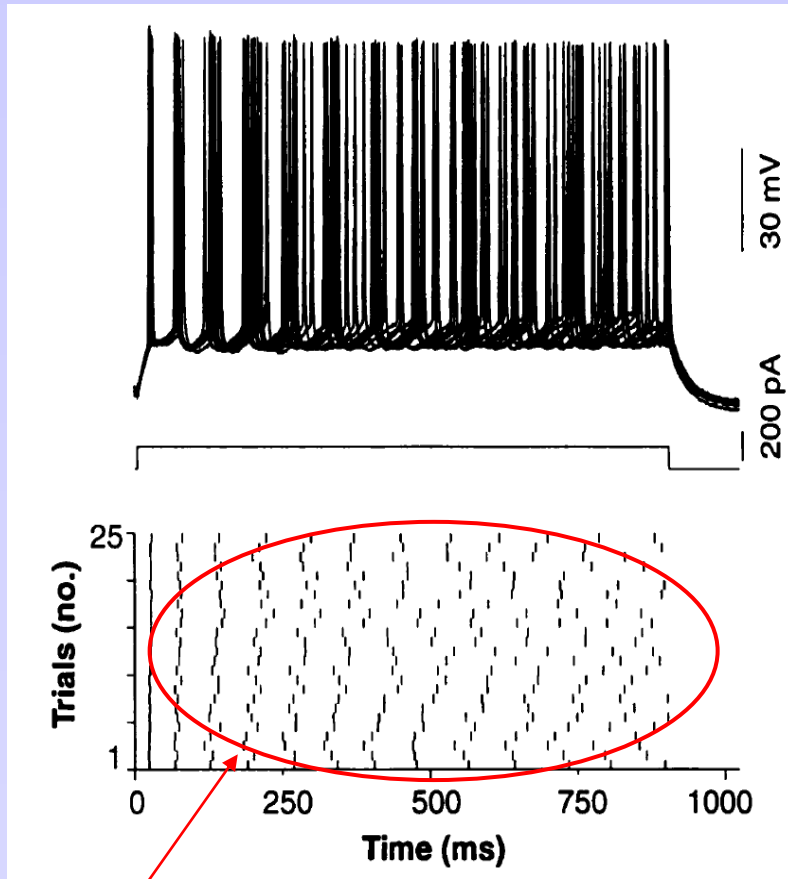
Noise is non-linearly voltage-dependent

(rat cortex, pyramidal cell, in vitro)

(Jacobson et. al. 2005)

- Does membrane noise matter?

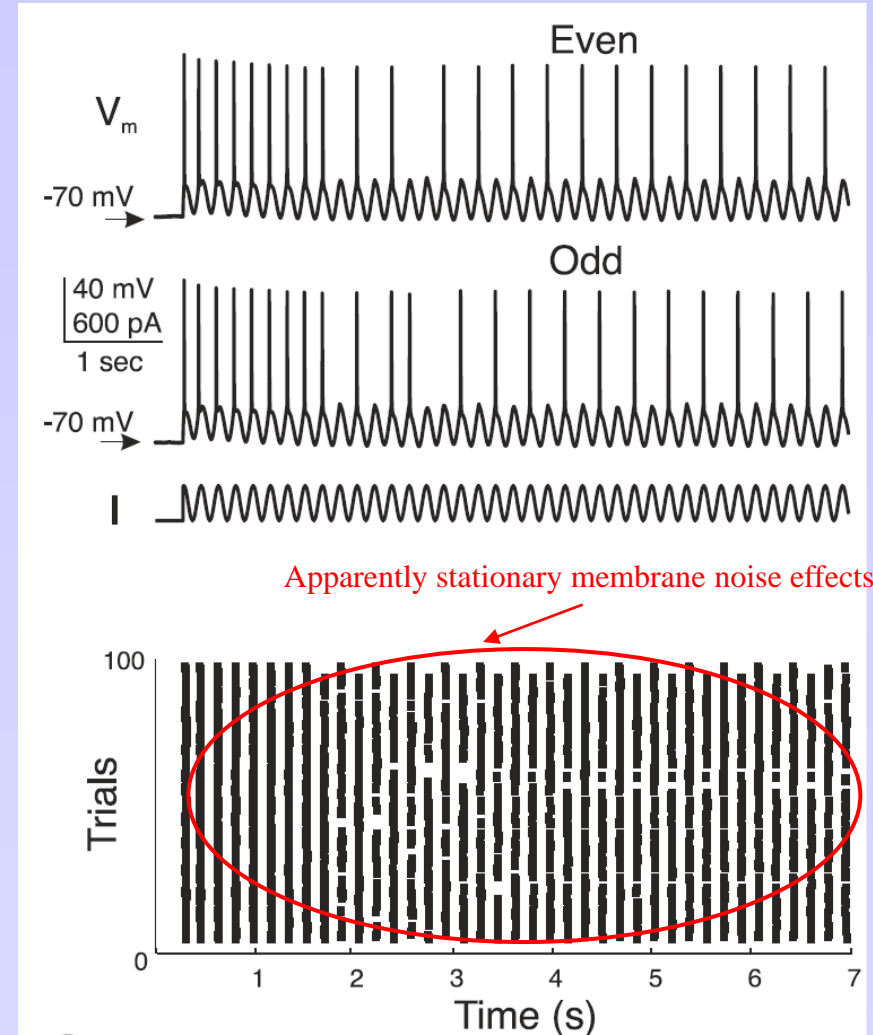
*Unstructured inputs*



(Mainen and Sejnowski, 1995)

Accumulating effects of membrane noise

*Structured inputs*

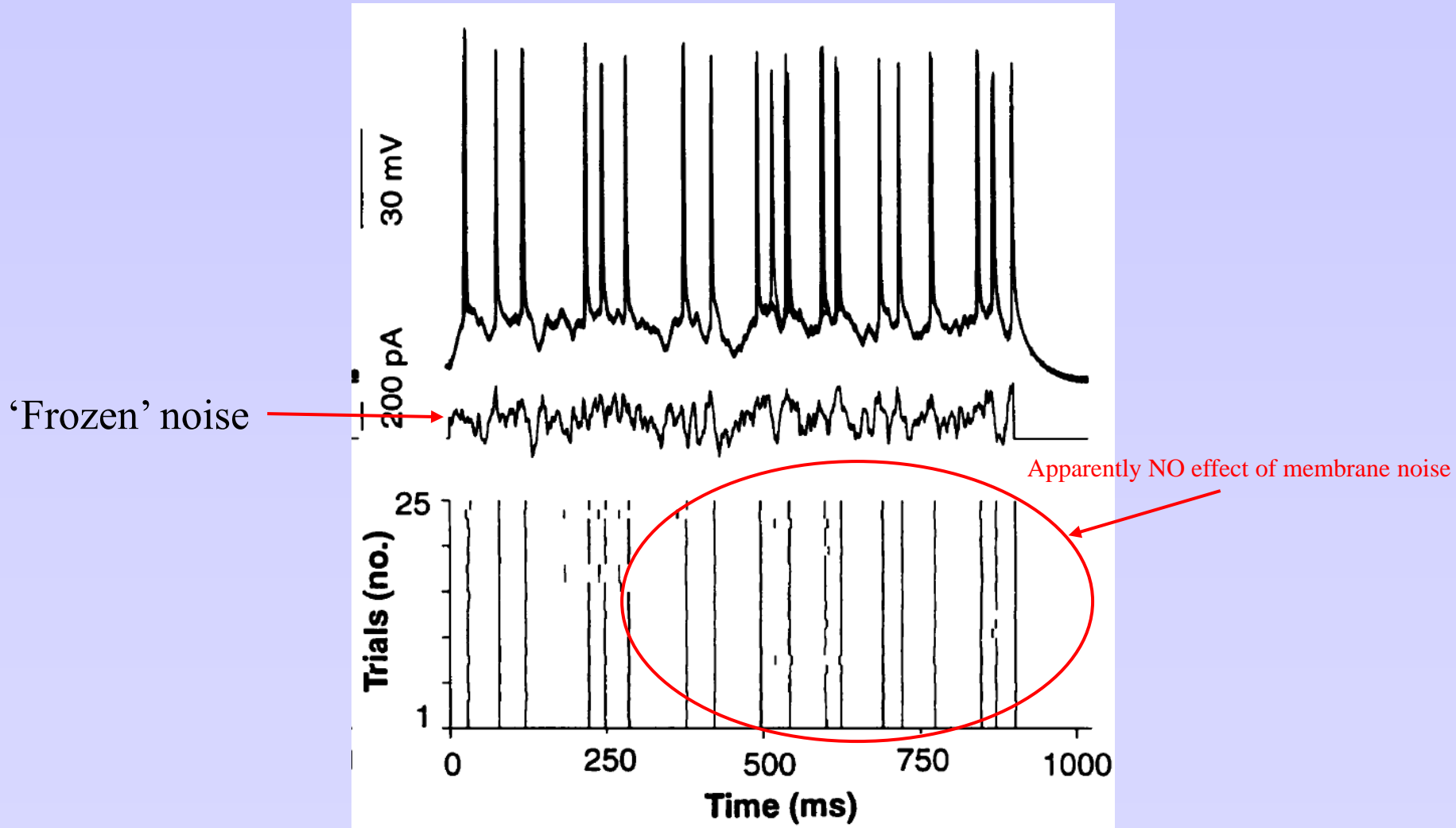


Rat prefrontal cortex pyramidal cells, in vitro, synaptic transmission blocked

(Fellous et. al. 2004)

# Spontaneous activity

- But!... What if the inputs are 'synaptic-like'



(Mainen and Sejnowski, 1995)

However.... Two Synaptic inputs are **NEVER** identical...

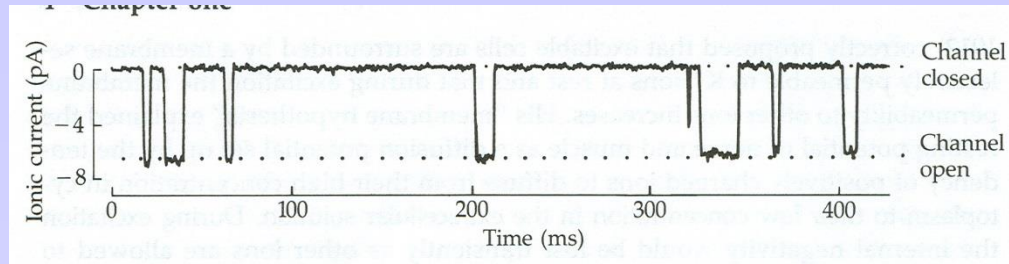
# Spontaneous Activity

Sources of noise: Intrinsic? Or Synaptic?

- Thermal noise ('Johnson' noise).

White noise, Gaussian amplitude distribution:  $\sim < 0.5 \text{ mV}$

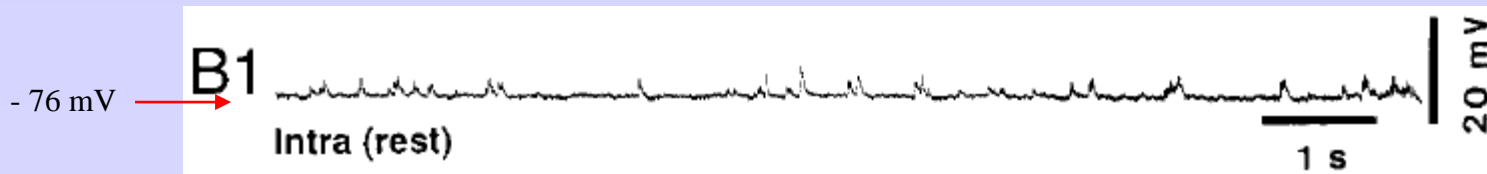
- Stochastic opening/closing of membrane channels:  $\sim < 0.5 \text{ mV}$



(Temperature dependent)

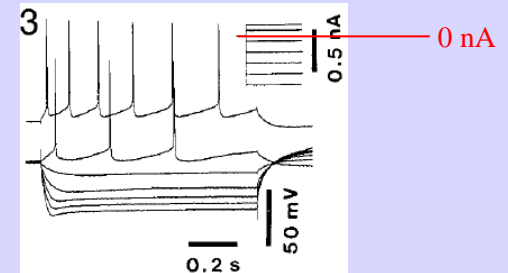
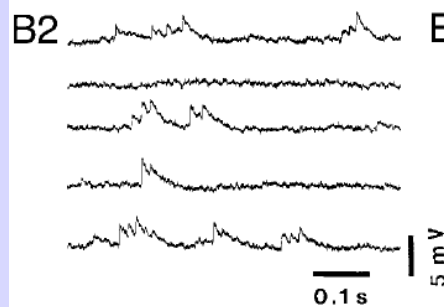
(Hille 2001)

- Synaptic noise:  $\sim 2-10 \text{ mV}$



*In vitro*

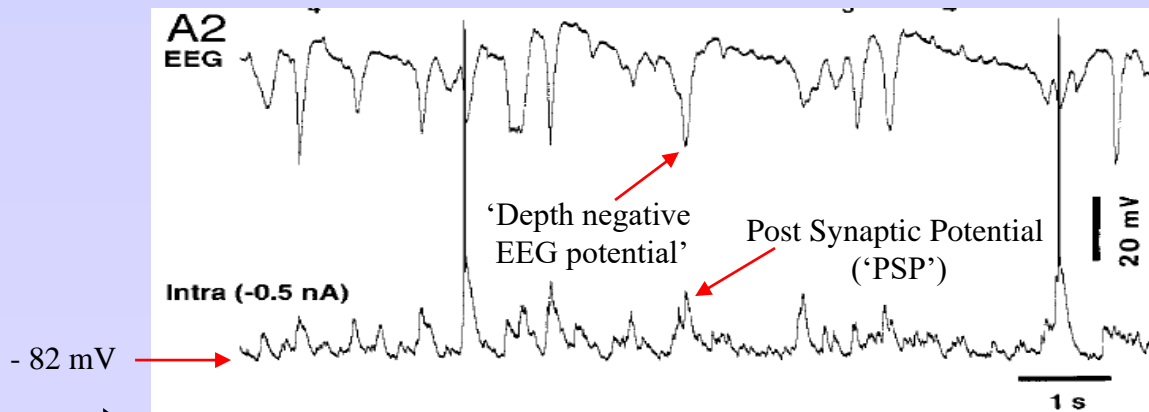
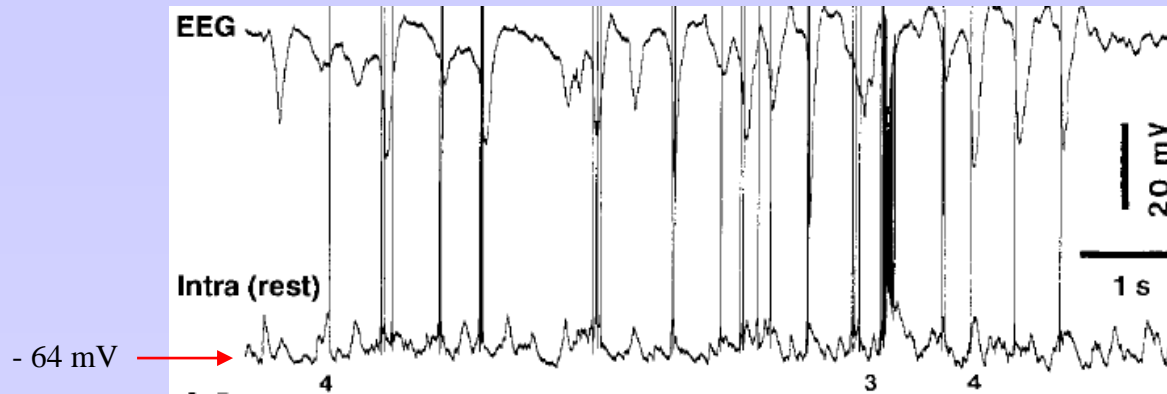
(Pare et. al. 1998)



Noise Vs APs

# Spontaneous Activity: Standard deviation of membrane potential

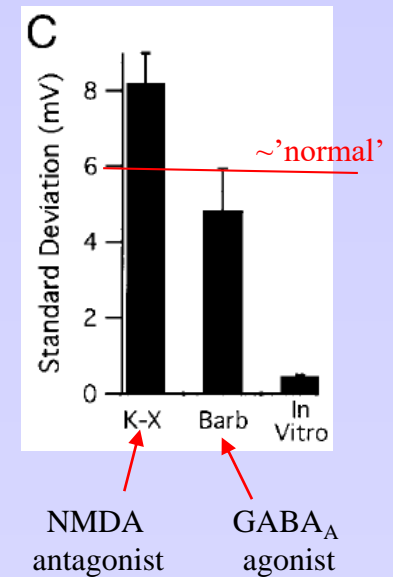
## Quantifying synaptic noise (in vivo)



(Pare et. al. 1998)

(hyperpolarized to better visualize spontaneous EPSPs)

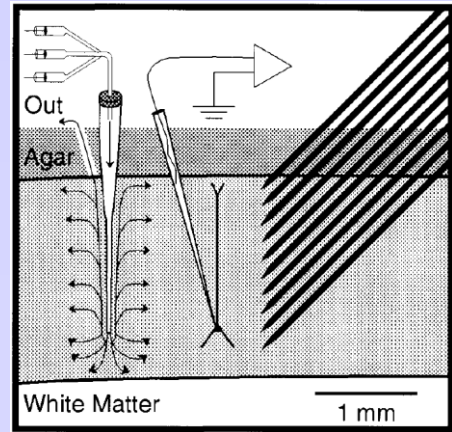
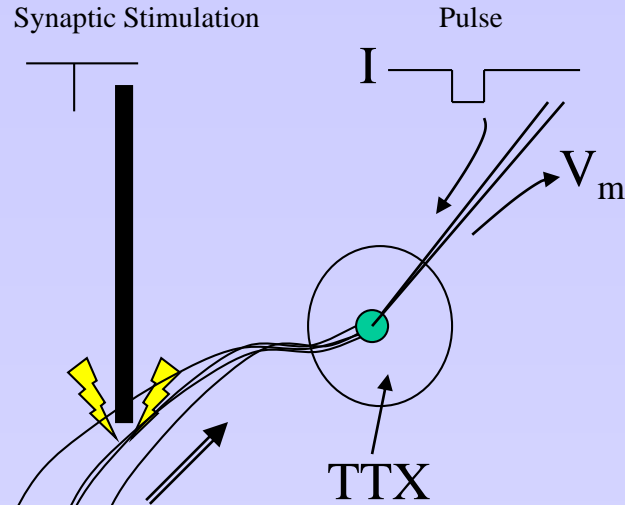
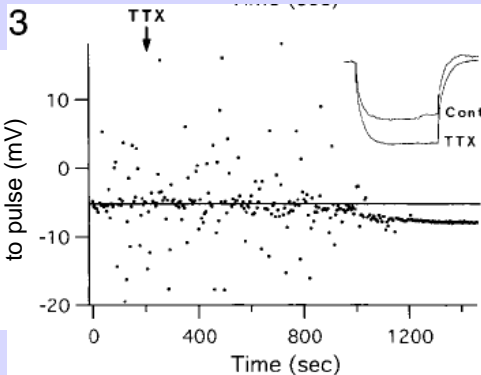
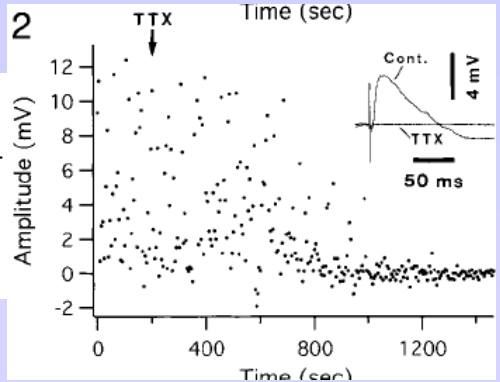
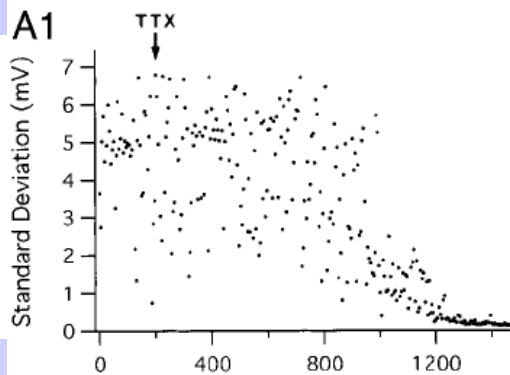
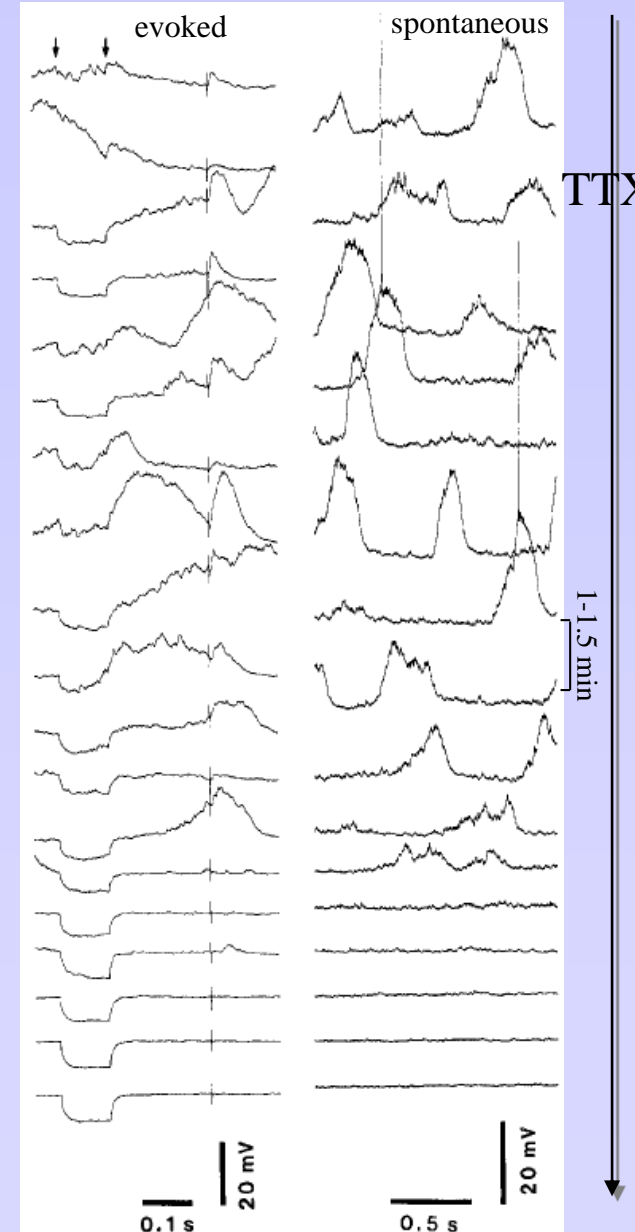
Note: convention:  
EEG downward → depolarizing potentials



Noise is anesthetics dependent

# The subthreshold effects of synaptic activity

TTX= blocks synaptic transmission



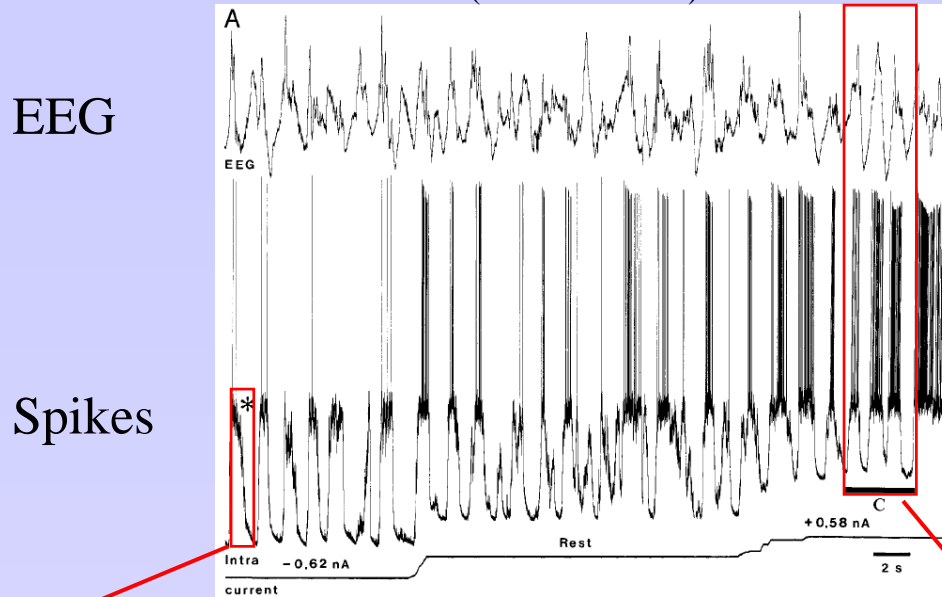
$$V_m = R_{in} I$$

→ Synaptic activity decreases Input Resistance

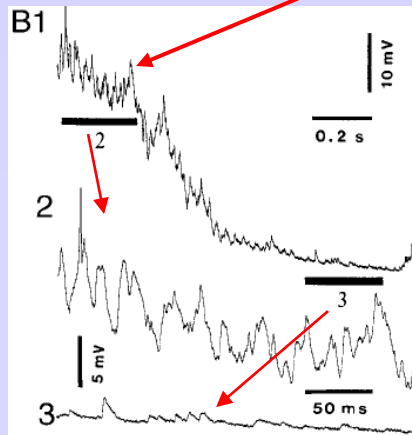
# Burst-iness

Burstiness (in mammalian cortex) is (mostly) a network phenomenon: Analyses of simultaneously sampled EEG and spike recordings.

(Pare et. al. 1998)

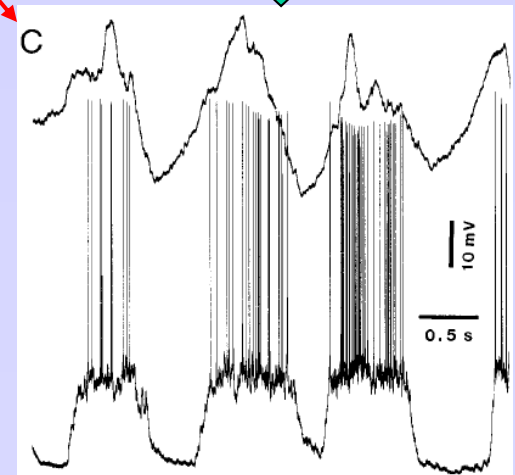


‘up’/‘down’ states  
‘slow oscillations’



Study of a cell at different holding voltages:

- ~Lower voltage (less GABA synaptic effects)
- ~Higher voltage (less AMPA synaptic effects)

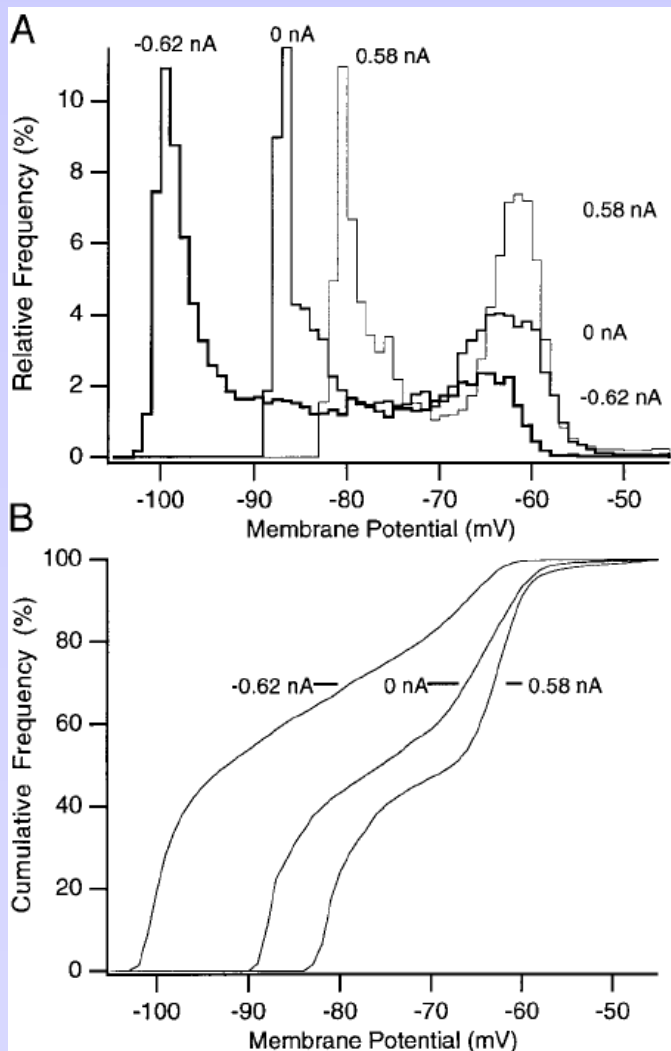




# Spontaneous Activity: Histogram of Membrane Potential

Is the standard deviation the best measure....?

Ketamine-Xylazine



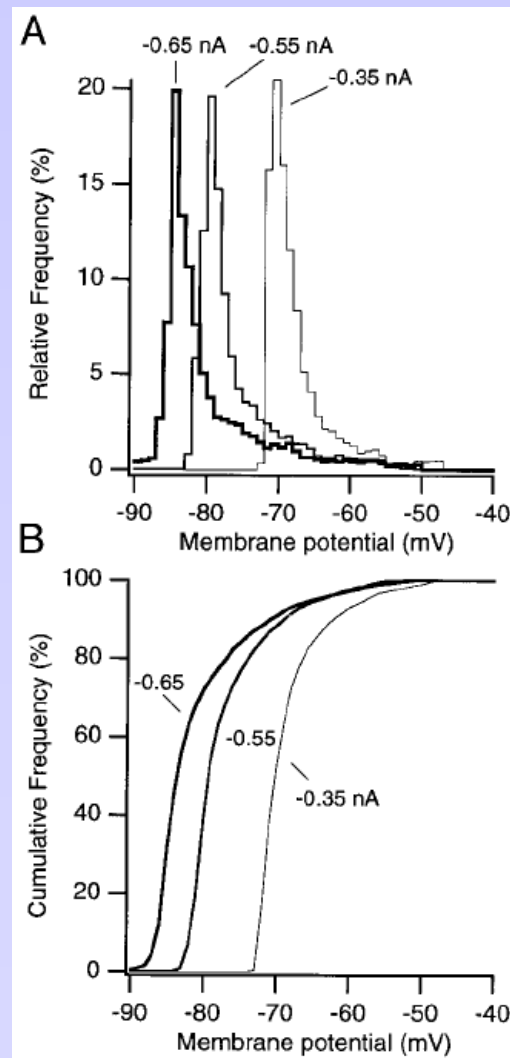
→ ‘visualizing’  
*distribution*  
shape change

Distributions:

Relative  
Vs  
Cumulative

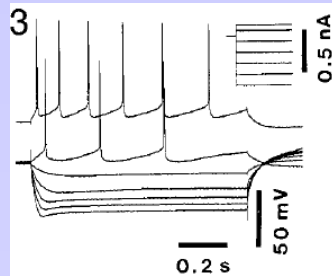
(Pare et. al. 1998)

Barbituate (pentobarbital)



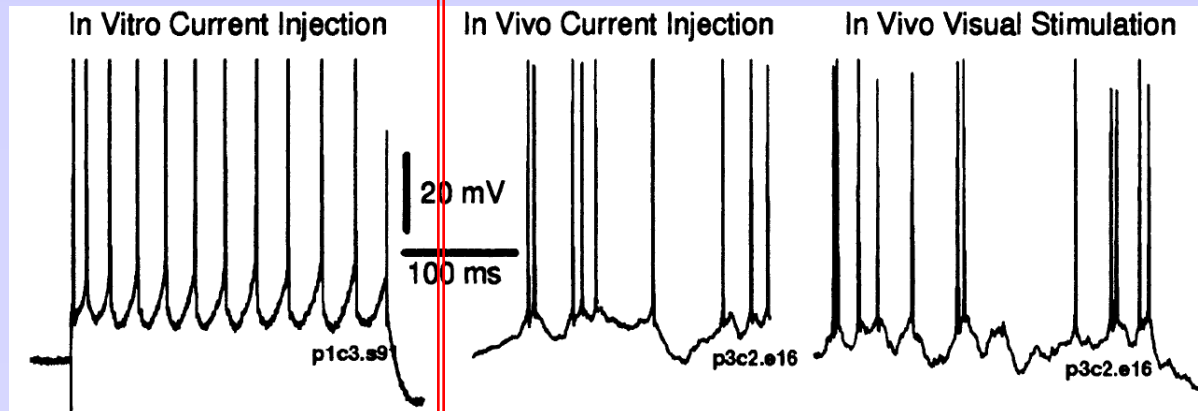
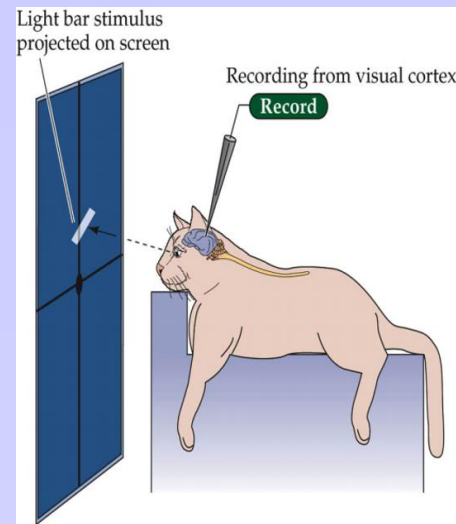
# Quantifying Spontaneous Spiking Activity

In vitro



(Pare et. al. 1998)

In vivo



(Holt et. al. 1996)

- Is there a number that can indicate whether a cell is firing regularly, randomly (single spikes) or randomly with bursts?

# Coefficient of Variation of ISIs

$$CV = C_V = \frac{\sigma_{ISI}}{\langle ISI \rangle}$$

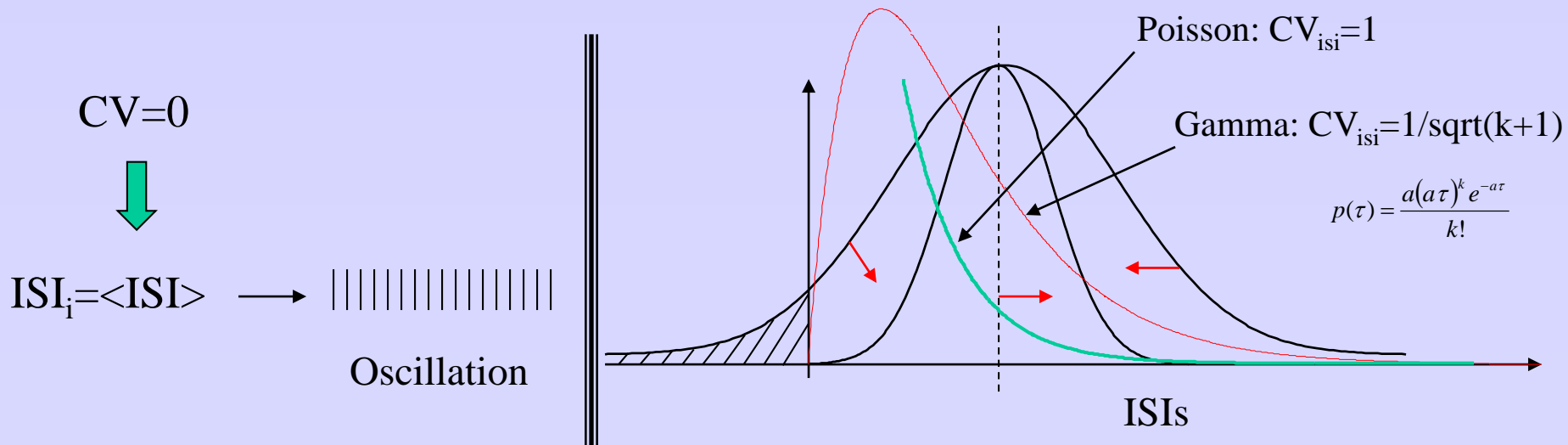
$$\sigma_{ISI} = \sqrt{\frac{\sum_{i=1}^N (ISI_i - \langle ISI \rangle)^2}{N}}$$

'true mean'

(note: biased Vs. **unbiased estimate of the variance**)

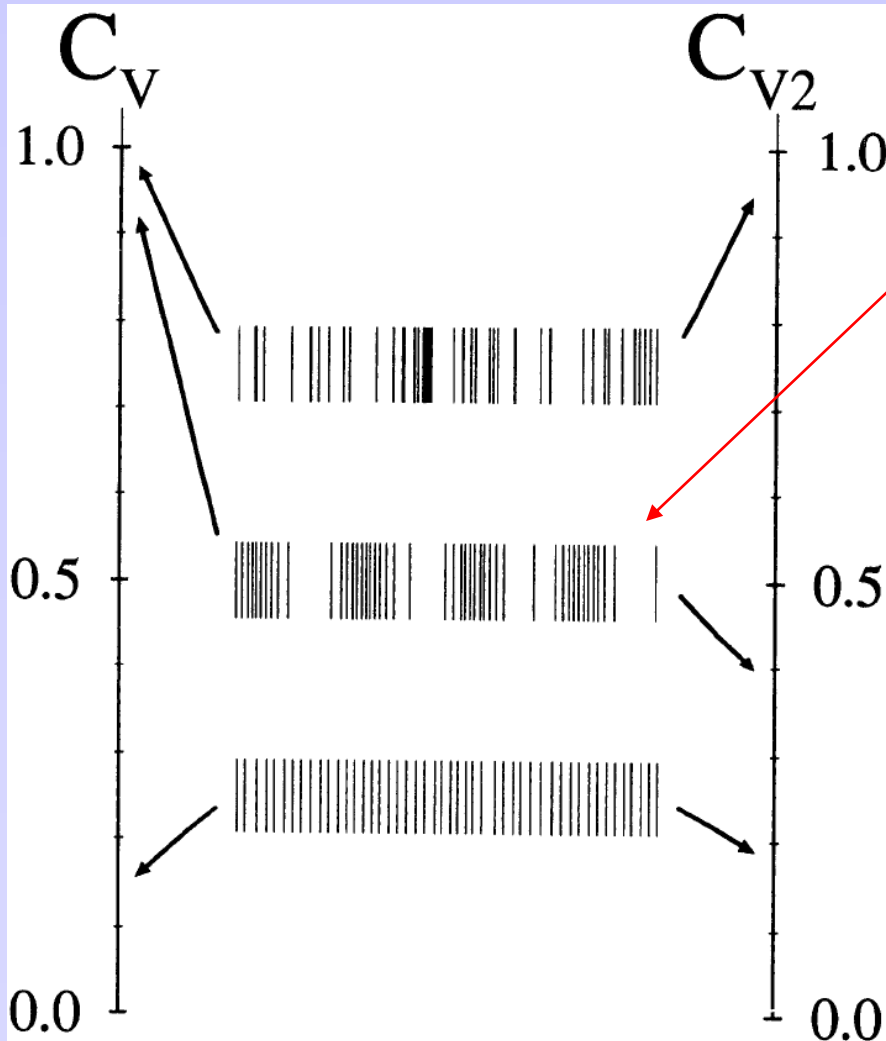
$$\sigma_{ISI} = \sqrt{\frac{\sum_{i=1}^N (ISI_i - \langle ISI \rangle)^2}{N-1}}$$

'sample mean'



# Coefficient of Variation of ISIs

- Is CV the best measure of variability/regularity?



(Holt et. al. 1996)

- The 'significance' of a variation should depend on the mean.
- Slow variations in firing rate should not 'count' as Poisson.

→ One possibility is to 'average' consecutive ISIs.

$$CV_2 = \frac{\sum_{i=1}^{N-1} \frac{2|ISI_{i+1} - ISI_i|}{ISI_{i+1} + ISI_i}}{N-1}$$

# Coefficient of Variation of ISIs

-When do we know we have a meaningful firing rate, CV, CV2?  $\Leftrightarrow$  When do we know we have **enough data**?

- Cumulative statistics approach:

(example: 200 spikes of a 20Hz Poisson train)

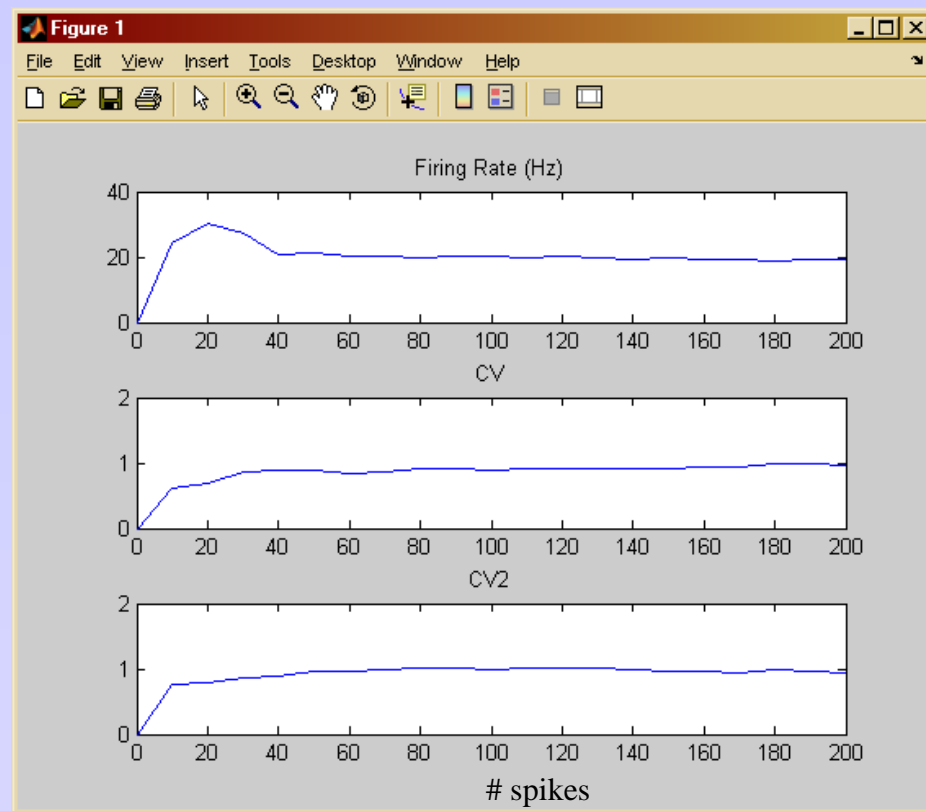
Algorithm.....

Take the first  $n$  spikes

compute/plot FR, CV, CV2

append the next  $(p)$  spikes to the list

stop if curve is 'stable', otherwise

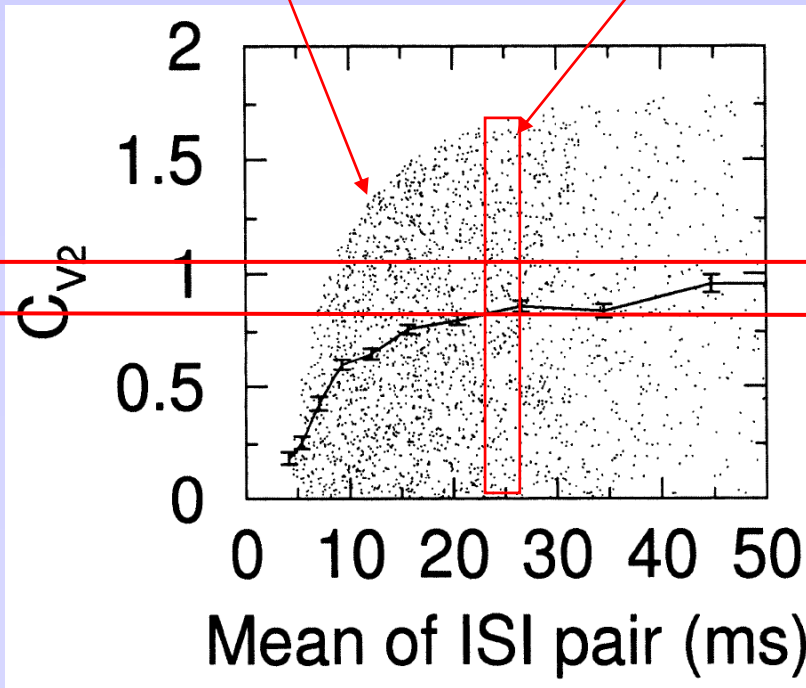


( $p=10$ )

# Coefficient of Variation of ISIs

- What is the shortest mean ISI that will be representative of the variability of the whole dataset? What is the time scale of variability?
- Part I: create and study a surrogate dataset

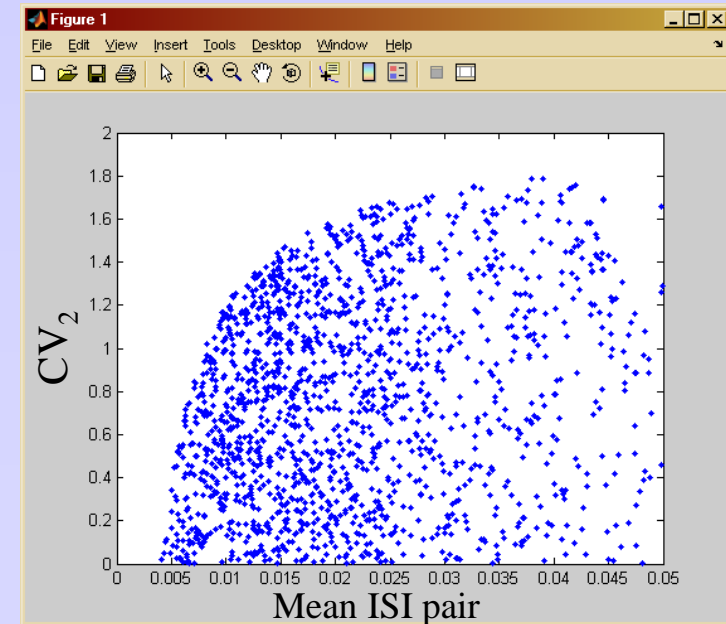
Boundary fit by  $2(1-t_r/x)$       uniform distribution  $\rightarrow$  Poisson



(Holt et. al. 1996)

$t_r$  = refractory period

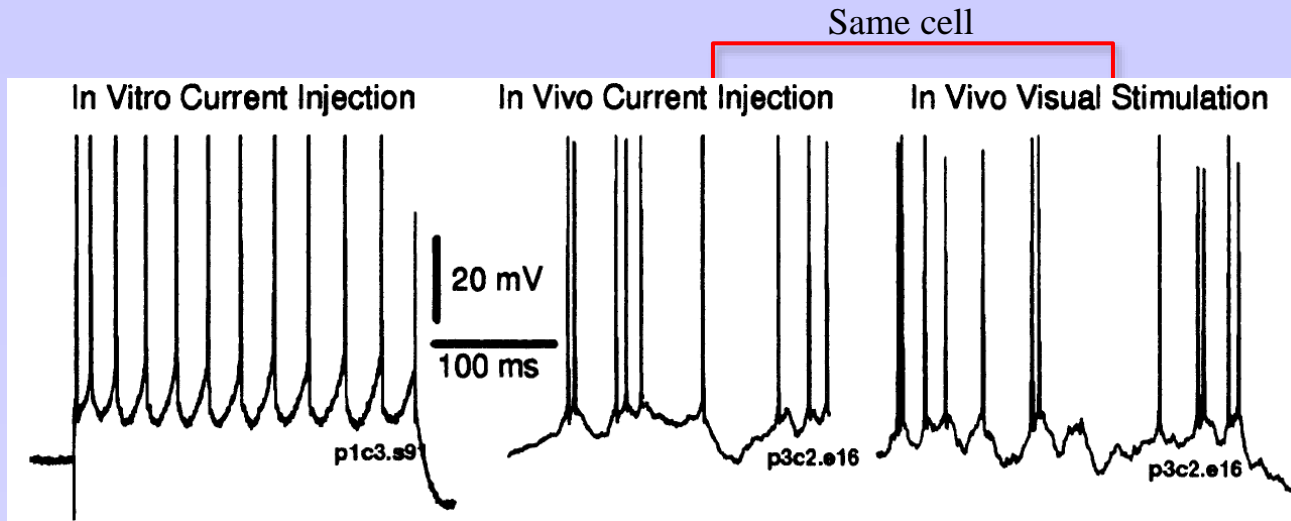
Is the data 'truly' random?



(2000 spikes, 50 Hz Poisson, 4ms refractory period)

# Coefficient of Variation of ISIs

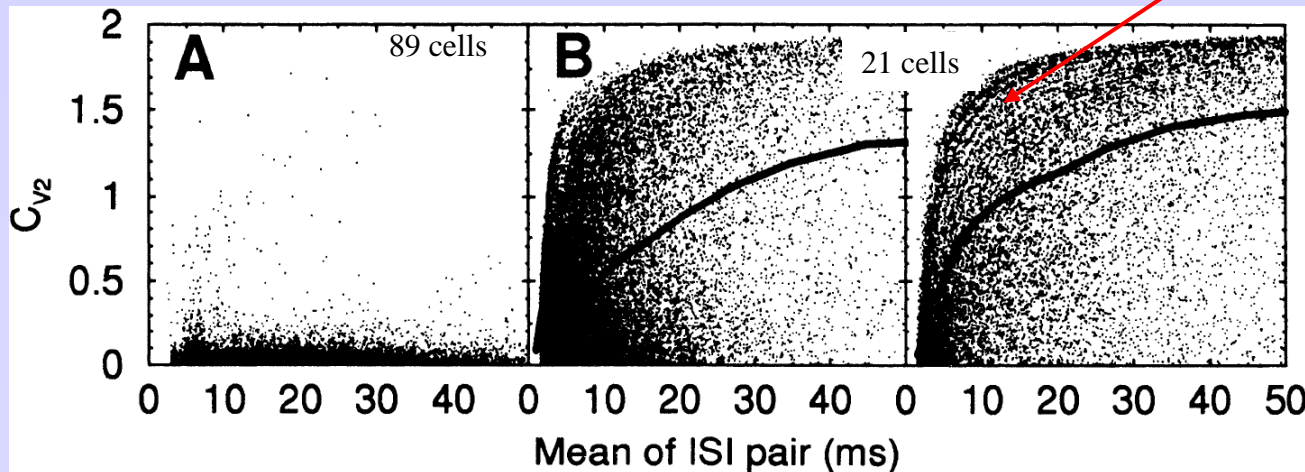
- Part II: Compare surrogate set with data



(Holt et. al. 1996)

- No *apparent* differences between current injection and visual stimulation? same FR, CV, mean  $CV_2$

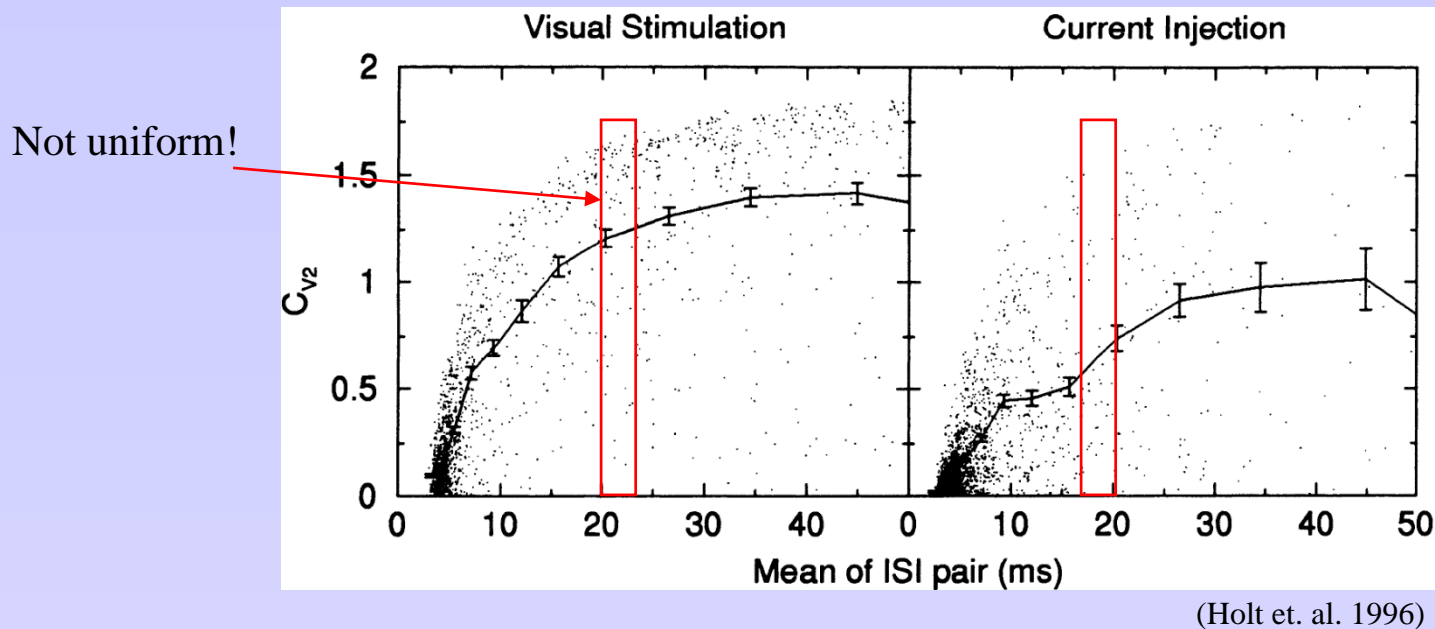
*Is this significant?*



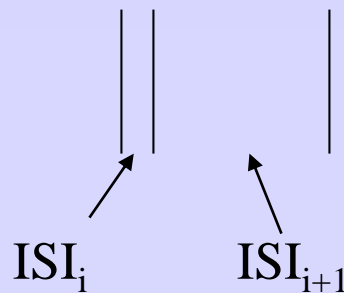
- Subtle (significant?) differences between  $CV_2$  curves

# Coefficient of Variation of ISIs

- Part III: Understand individual cases



$$CV_2 = \frac{\sum_{i=1}^N \frac{2|ISI_{i+1} - ISI_i|}{ISI_{i+1} + ISI_i}}{N}$$

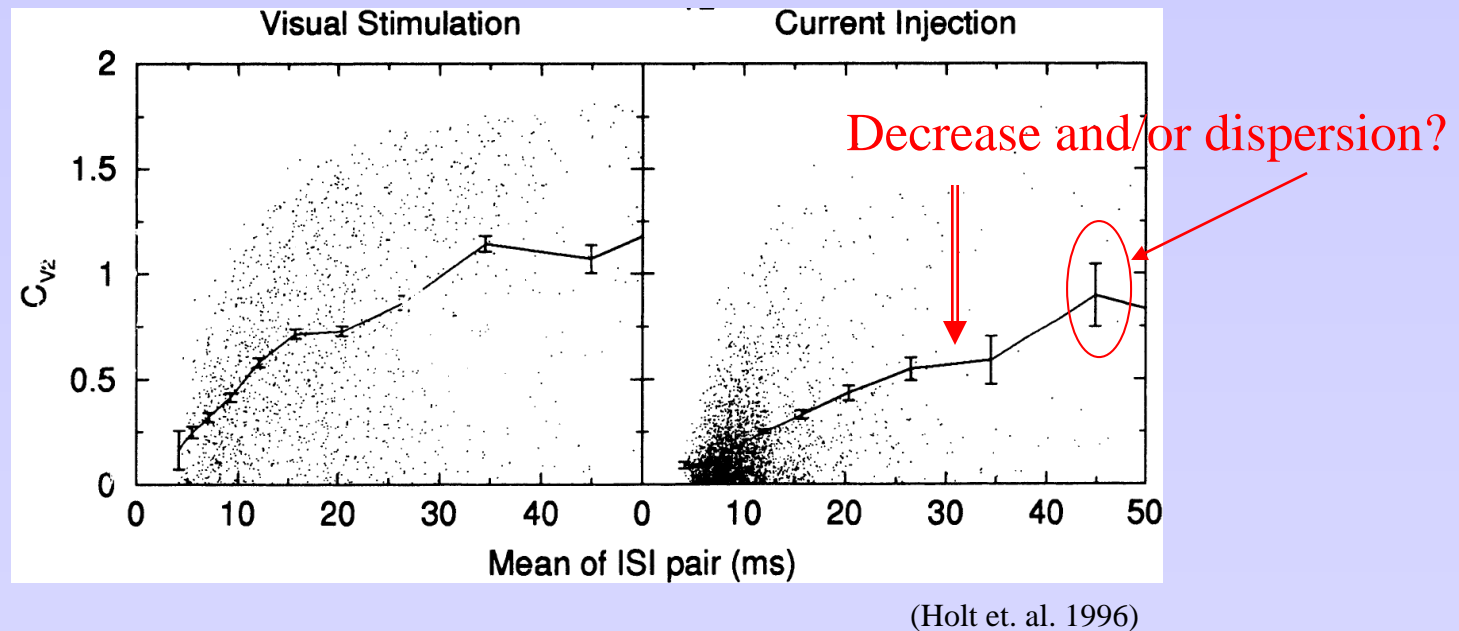


Bursty cell with visual stimulation, but not with current injection



# Coefficient of Variation of ISIs

- Check.... Non bursty cell



For cells that are not bursty,  $CV_2$  decrease during current injections (i.e. cells are more regular at short mean ISIs)

# Coefficient of Variation of ISIs

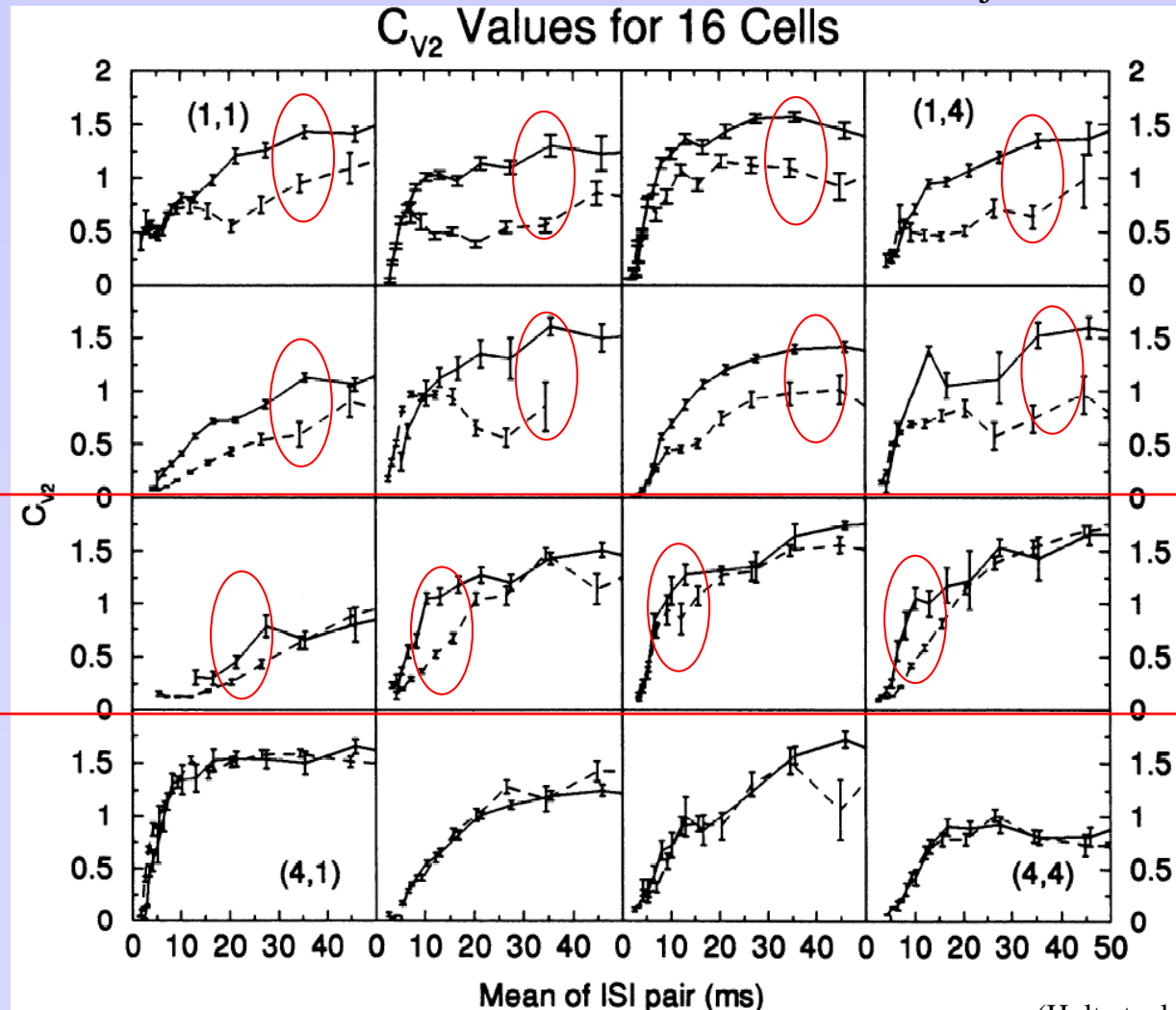
- Population analyses: What do the differences mean?

Visual stimulation ———  
Current injection - - - - -

Long ISIs  
(more bursty during  
visual stimulation)

Short ISIs  
(relative refractory  
period differences?)

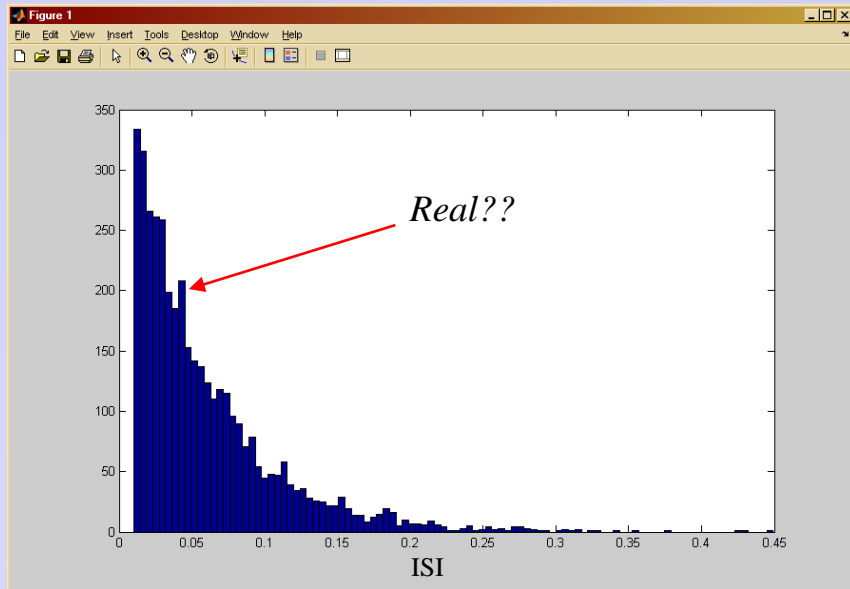
Same



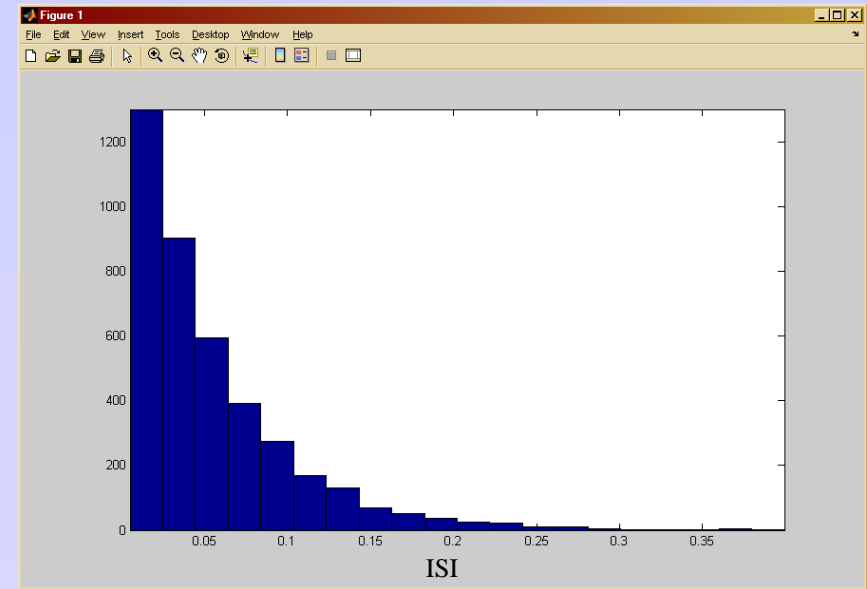
# Distribution of ISIs

Side Note: Warning!: Beware of Binning artifacts...

$\text{binsize} > \text{Refractory\_Period}$



10ms refractory period, 5ms bins



10ms refractory period, 25ms bins

More on this later....

# ISI return map

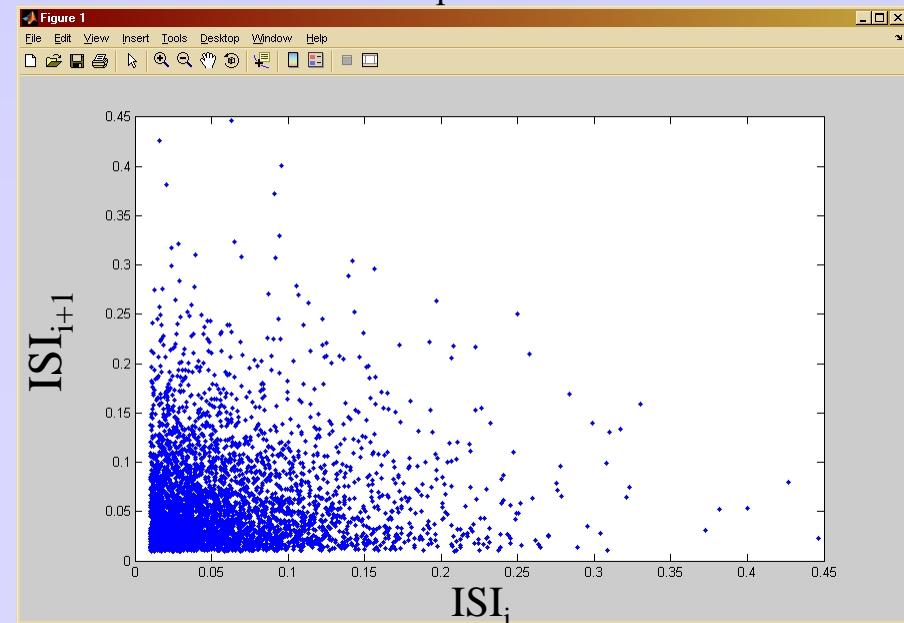
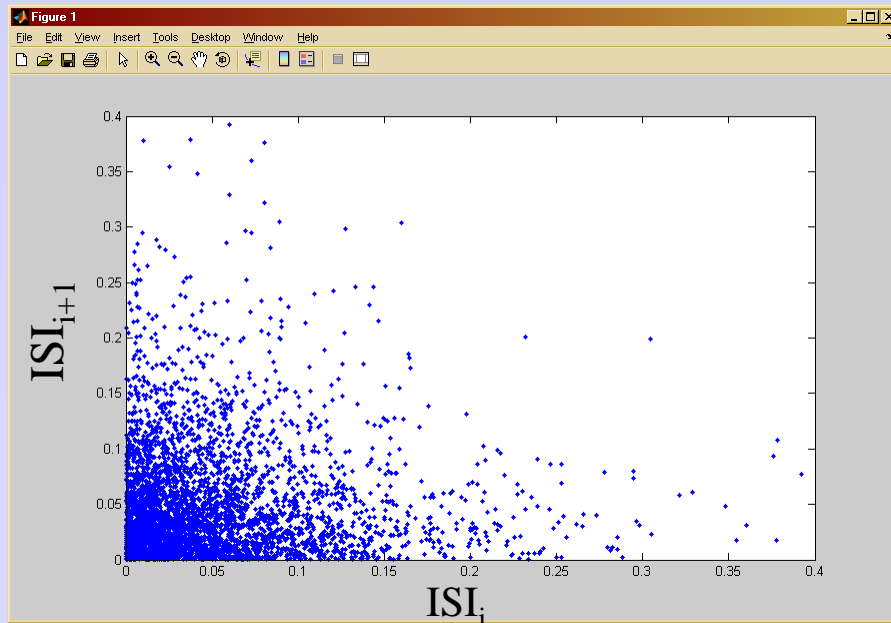
- FR, CV, CV<sub>2</sub> are ‘overall’ spike train measurements
- Goal: Detecting irregular (i.e. not visible ‘by eye’) temporal structure in spike trains



Henri Poincaré  
(1854-1912)

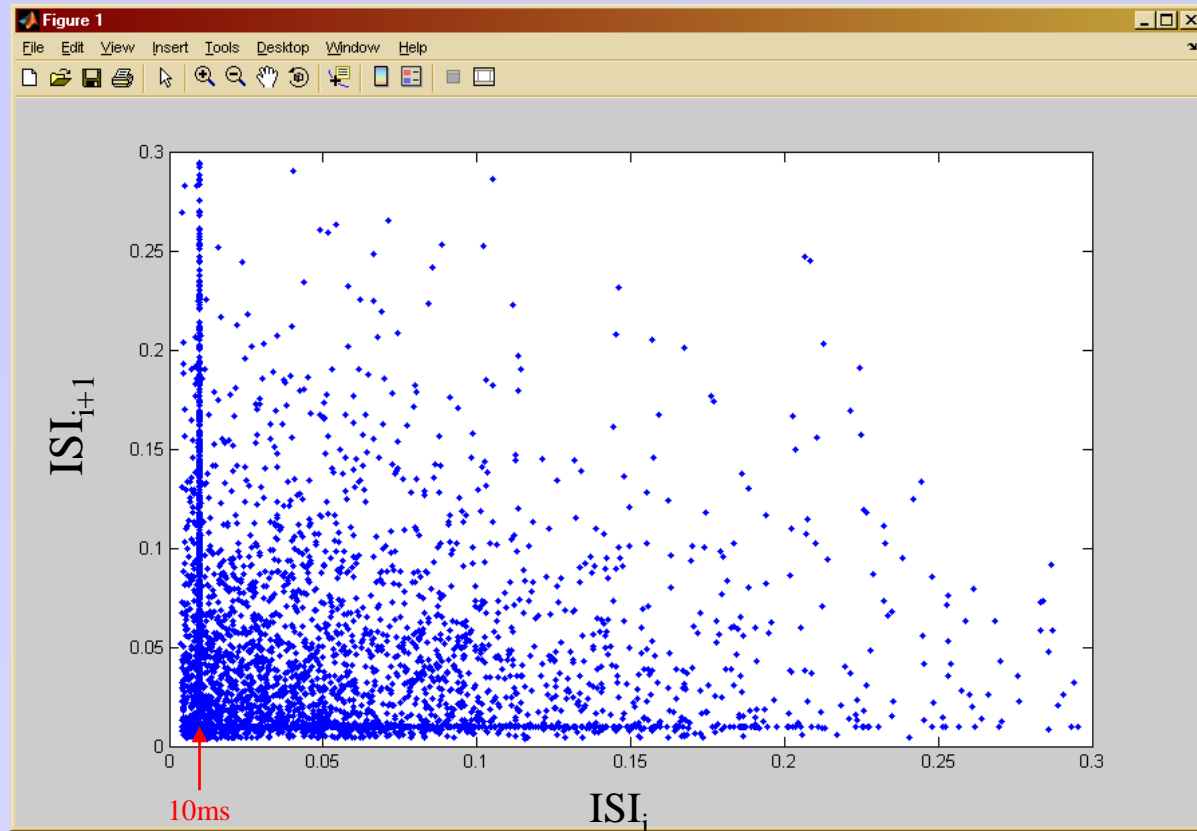
→ Poincaré map – ISI return map

Find and interpret the difference....

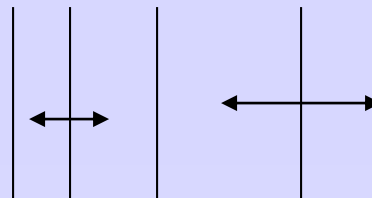
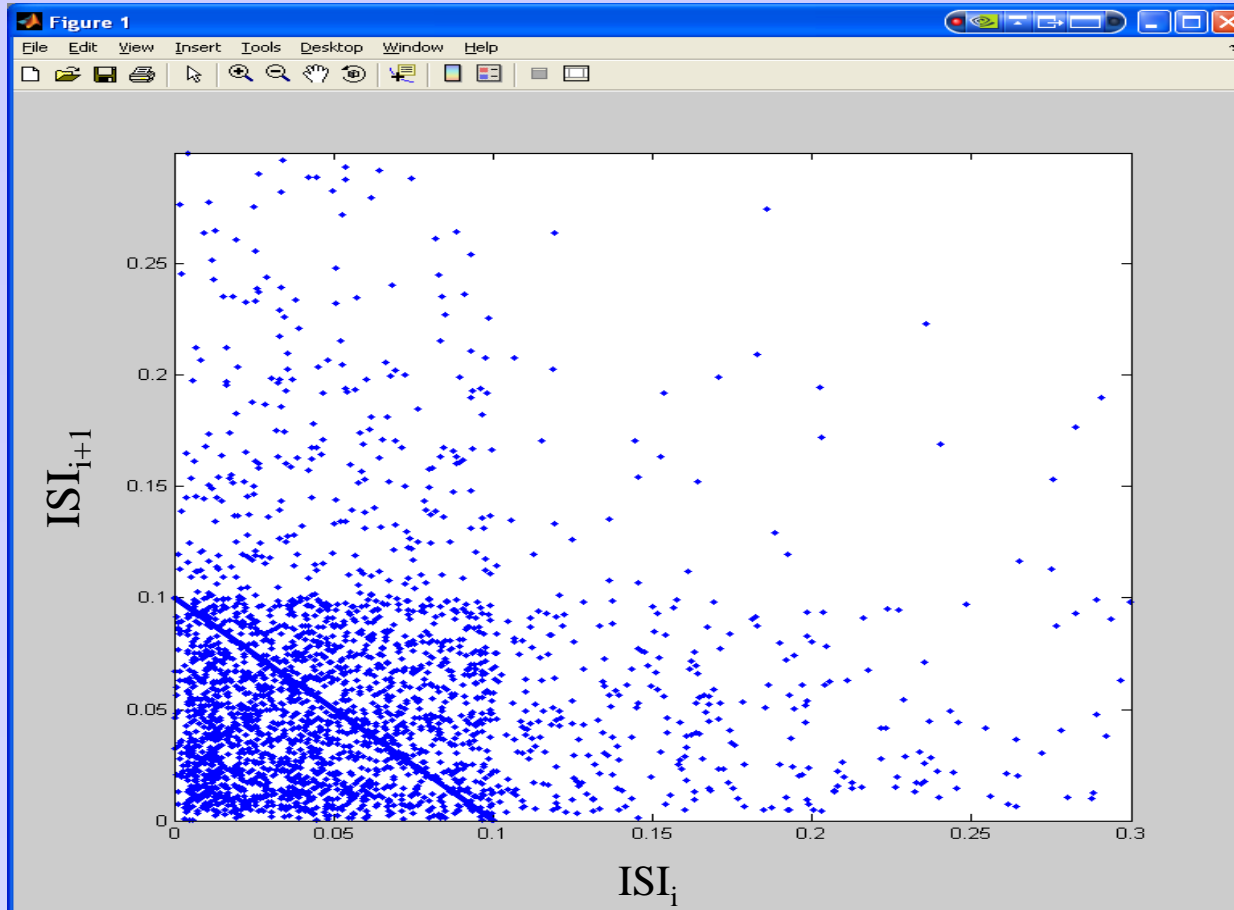


(20 Hz Poisson train)

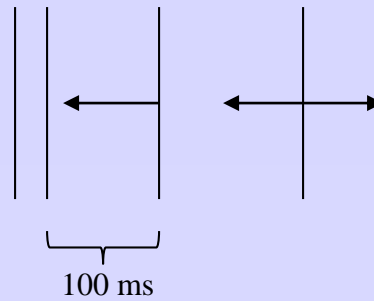
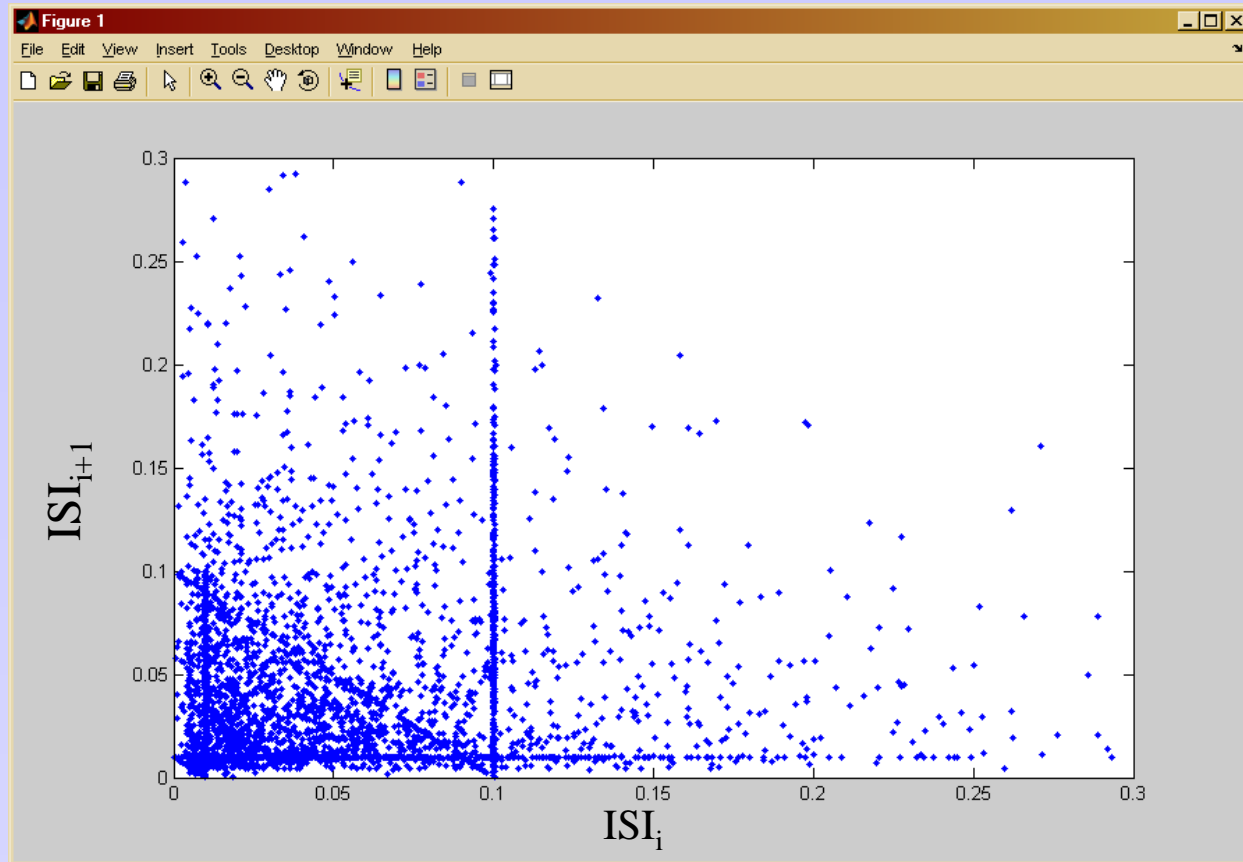
# ISI return map



# ISI return map

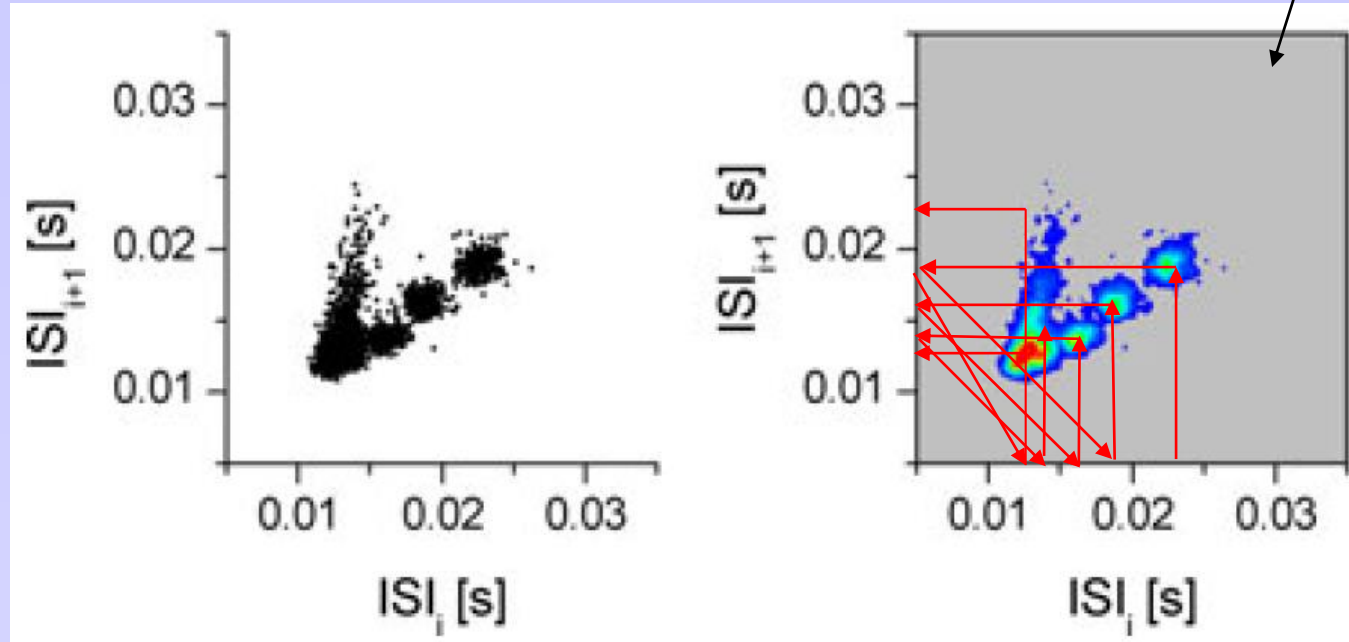


# ISI return map

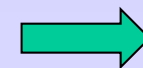
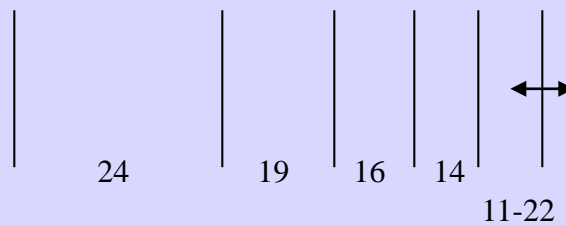
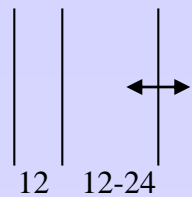


# ISI return map... for real

Pyloric neuron lobster STG



(Szucs et. al. 2005)

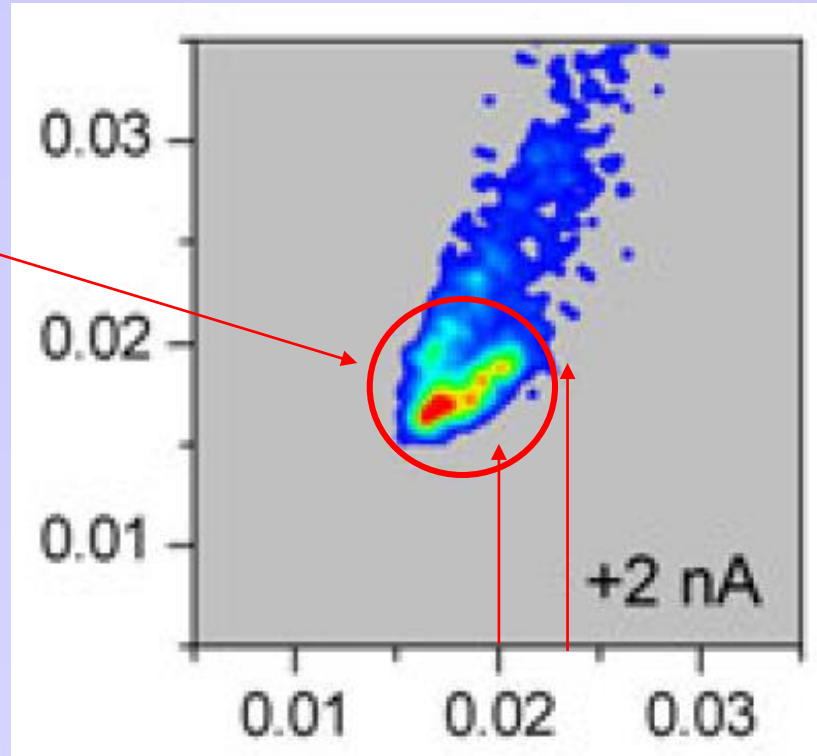


Two types of bursts

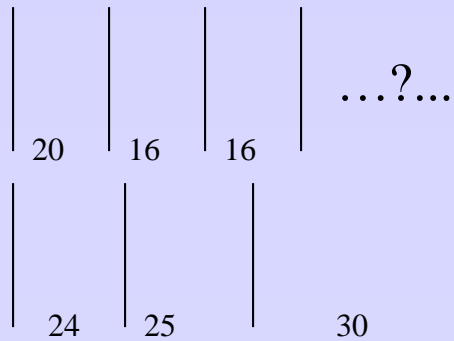


# ISI return map... for real

Attractor



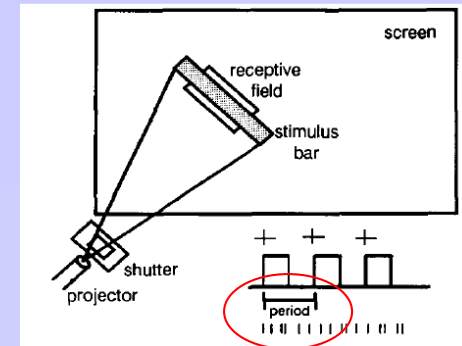
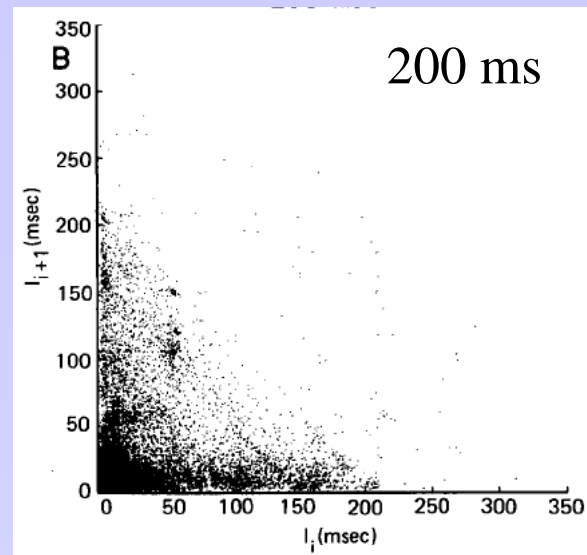
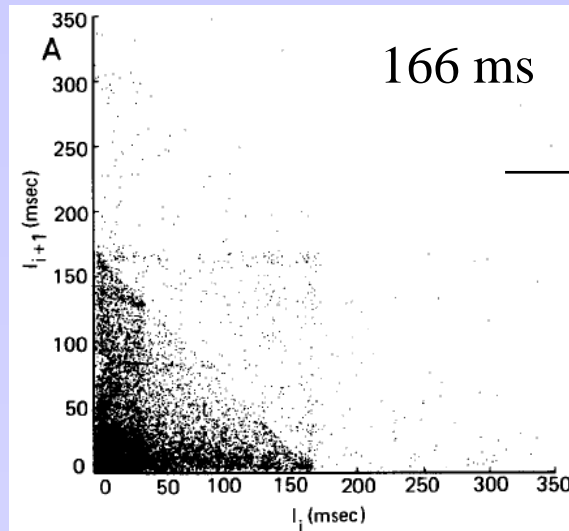
(Szucs et. al. 2005)



Two types of bursts

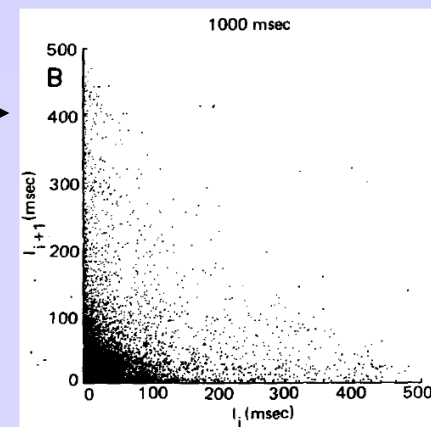
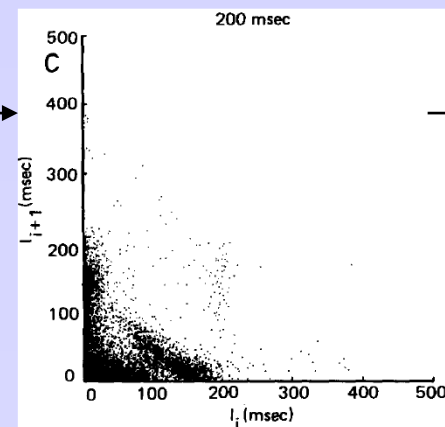
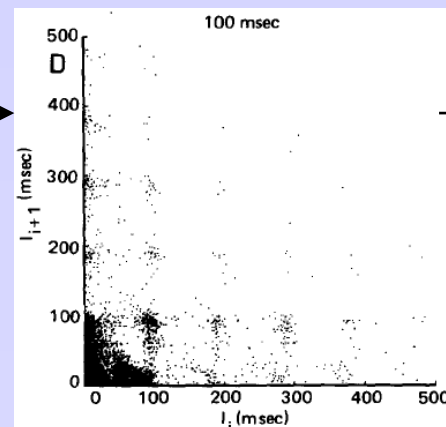
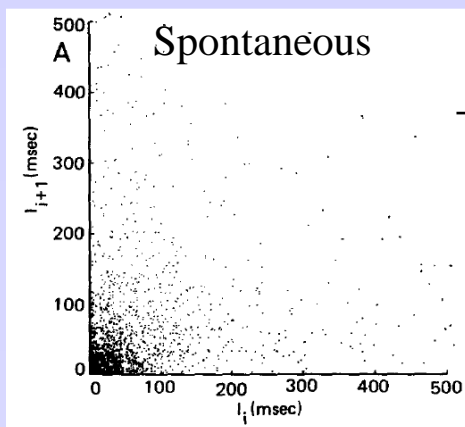
# Other real ISI return maps

## Stimulus-triggered Return Map



Stimulus  
period

(Siegel, 1990)



# Fano Factor – a.k.a. ‘index of dispersion’

- Measure the presence (and time scale) of intrinsic temporal correlations in a spike train.

- If one measures the distribution of the number of spikes occurring in  $T$  seconds (as a result of different experimental conditions for example):

$$FF(T) = \frac{\sigma^2(T)}{\mu(T)}$$

← Variance of ISI in T  
← Mean of ISI in T

- For a Poisson distribution:  $FF(T)=1$

- For a *renewal* process and large enough  $T$

$$\mu(T) \cong \frac{T}{\langle ISI \rangle} \qquad \sigma(T) \cong \sqrt{\frac{T \sigma_{ISI}^2}{\langle ISI \rangle^3}}$$

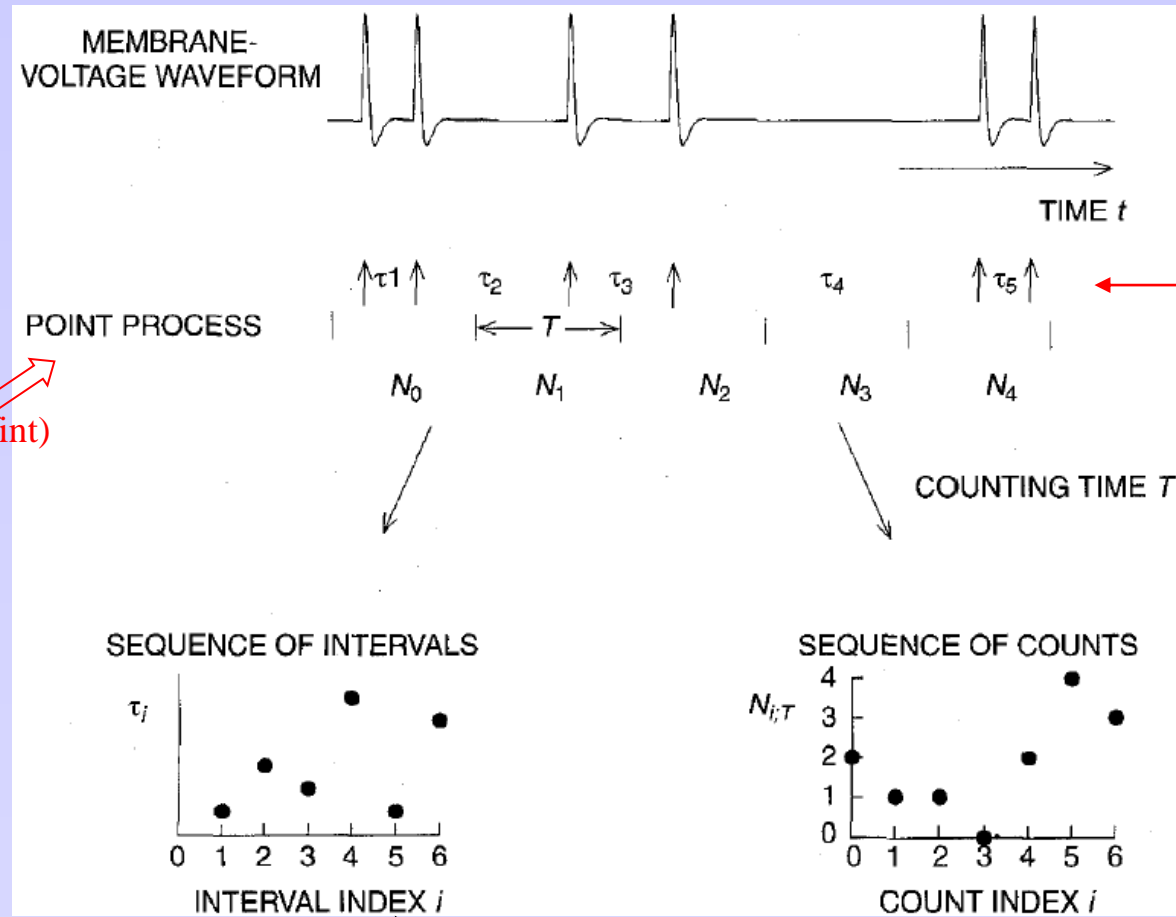
$$FF(T) = \left( \frac{\sigma_{ISI}}{\langle ISI \rangle} \right)^2 = CV_{ISI}^2$$



Ugo Fano  
(1912-2001)

# Fano Factor

Fano factor uses spike counts, not ISIs



(spike = 1 time point)

ISIs

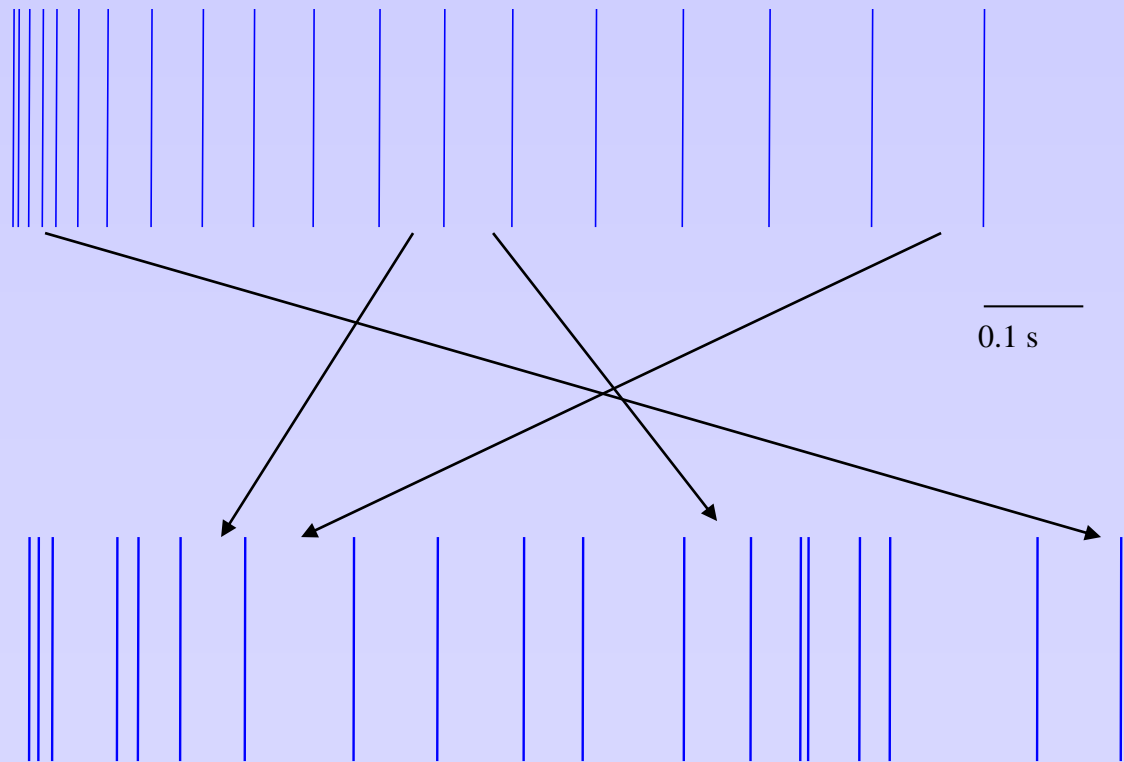
'Recoding'

ISI Vs. Count

(Teich. al. 1996)

# 'Cheap' Surrogate Dataset: Shuffled ISI

Shuffling does not change ISI distribution (Poisson  $\rightarrow$  Poisson)

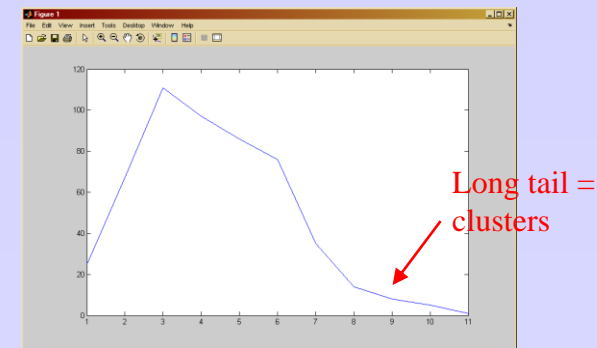
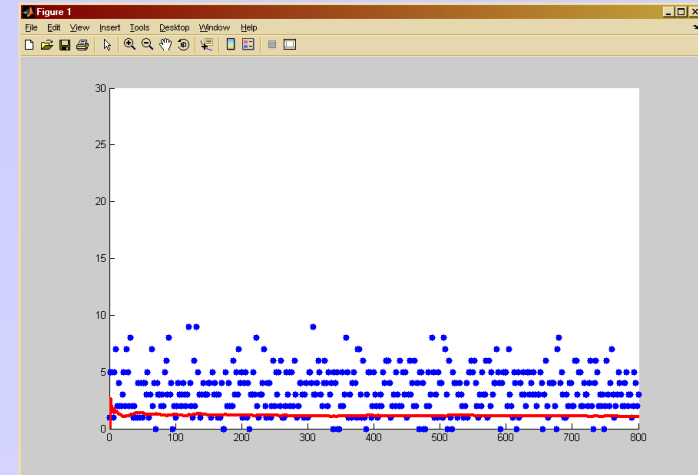
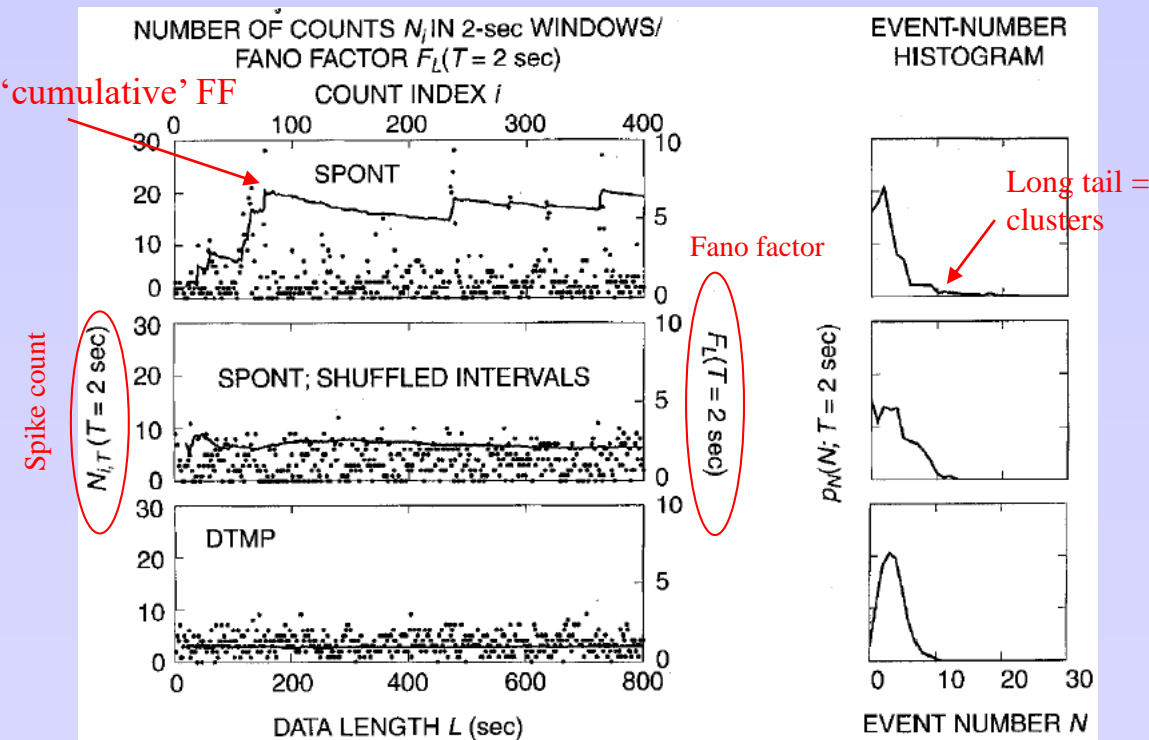


# Fano Factor

- Data (cat V1) Vs. Shuffled data Vs. Poisson: Testing significance

Simple (in vivo) Neuron Model

Spontaneous -  $T=2$  sec

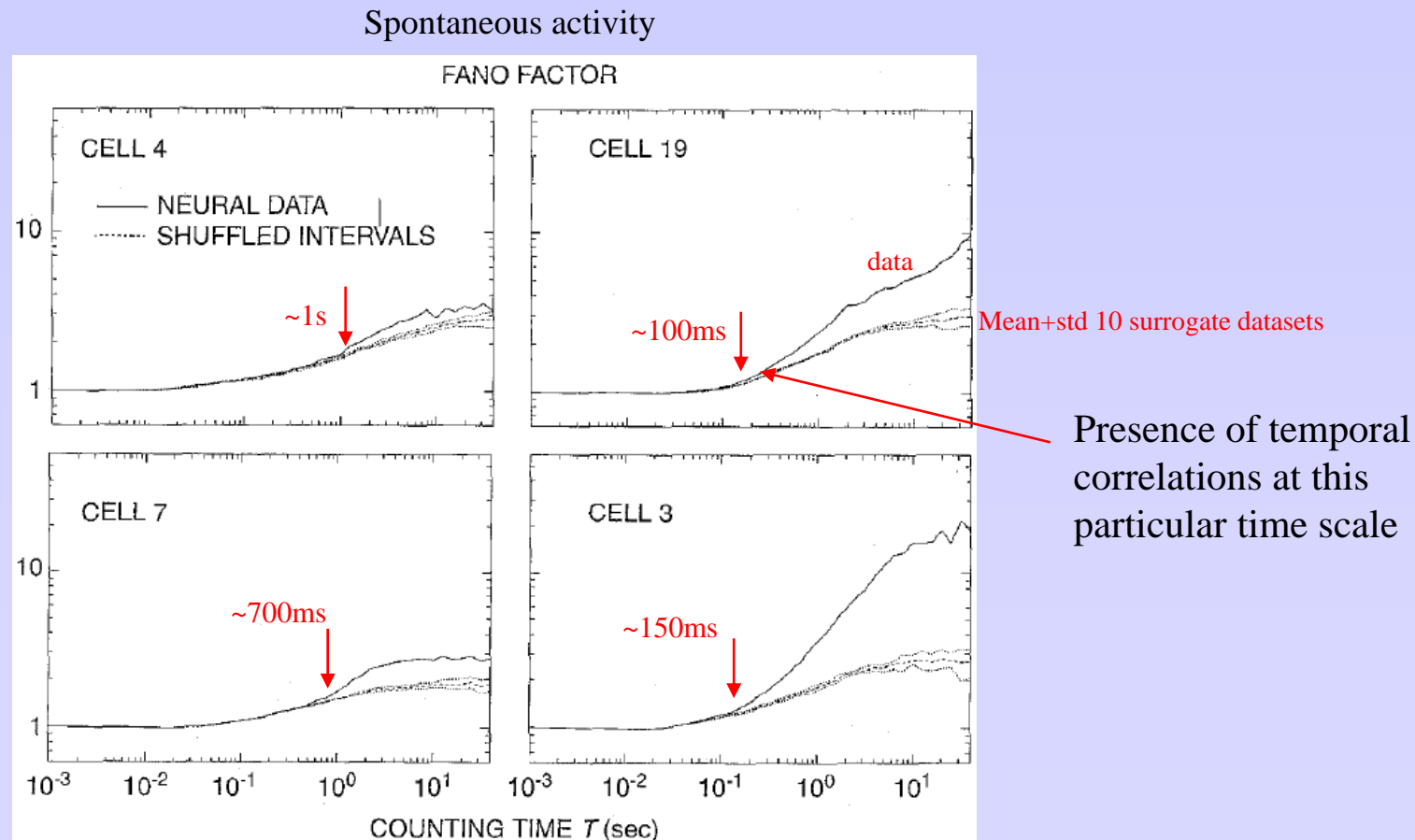


(Teich. al. 1996)

➔ FF jumps when spikes cluster, or when spikes 'de-cluster'

# Fano Factor

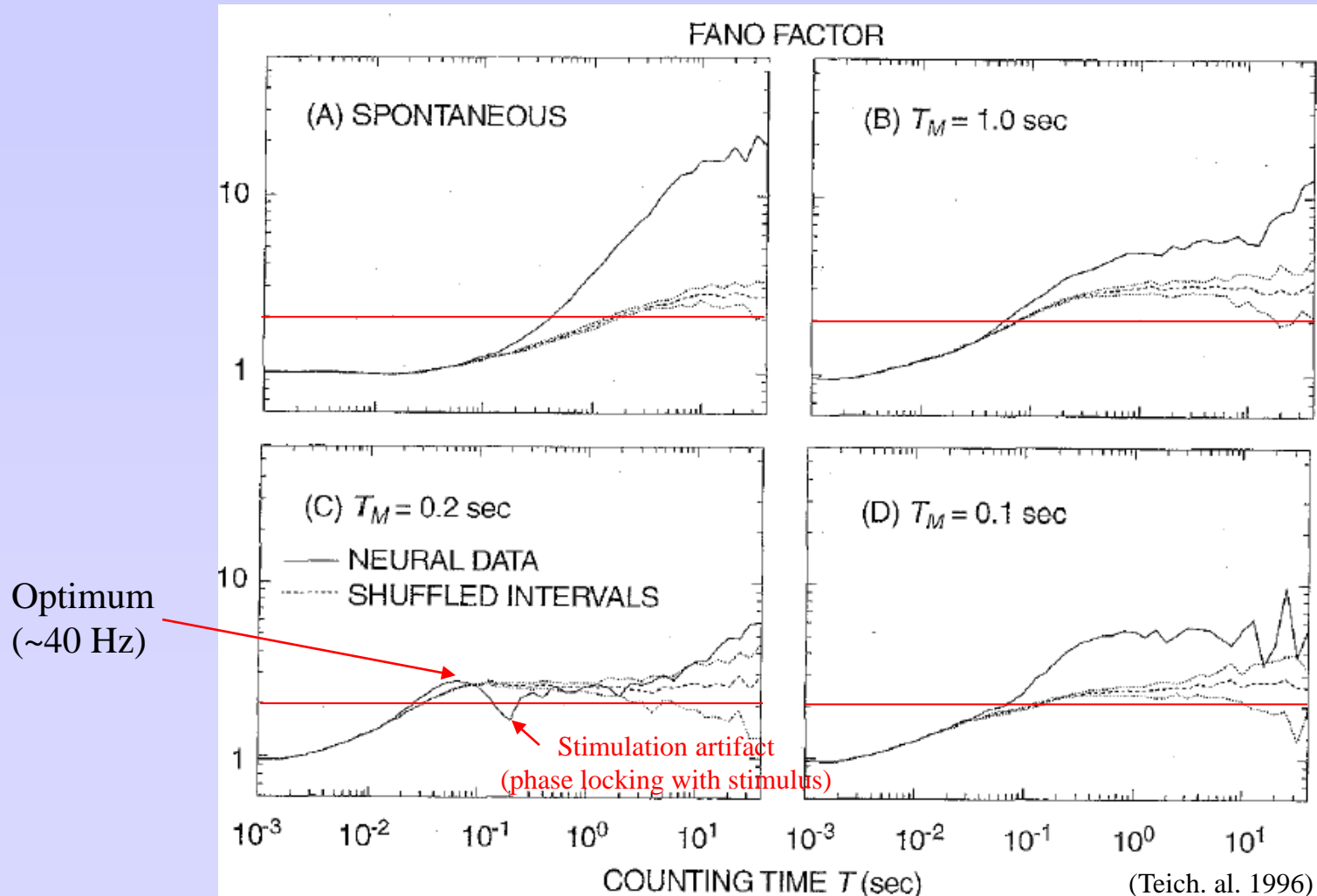
- Because FF depends on  $T$ , one can study the statistics of the spontaneous activity at *specific* time scales.
- Use of shuffled ISIs as a surrogate dataset.



(Teich, al. 1996)

# Fano Factor

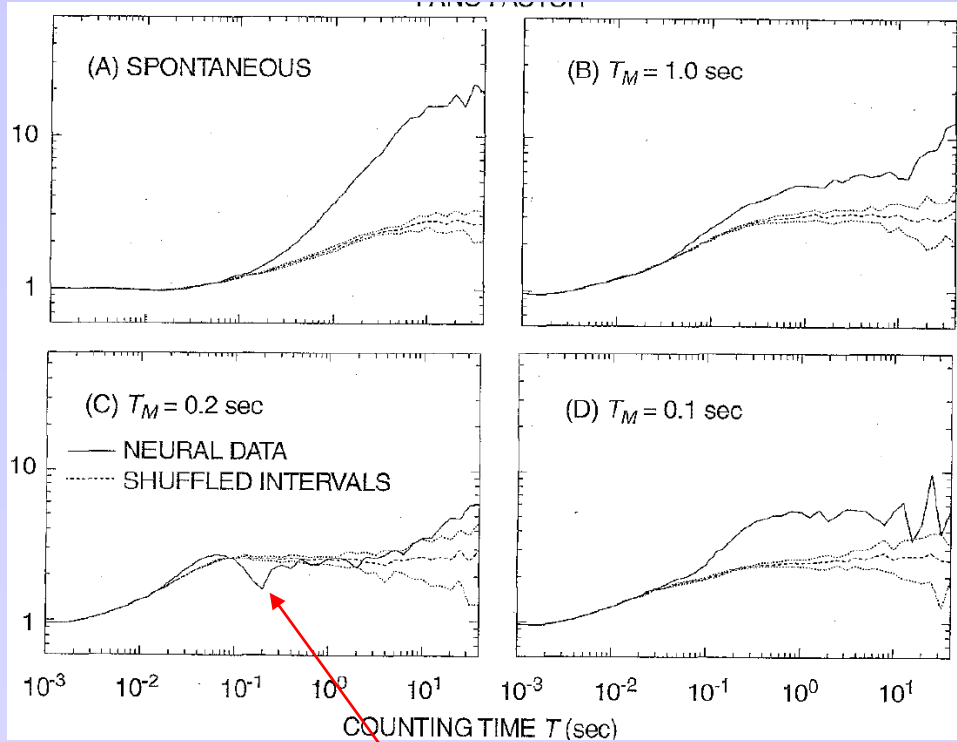
- Fano factor during visual stimulation at 1 Hz, 5 Hz and 10 Hz
- $FF > 2 \Leftrightarrow CV > 1.4$  ... Presence of 'clustering' in spike train



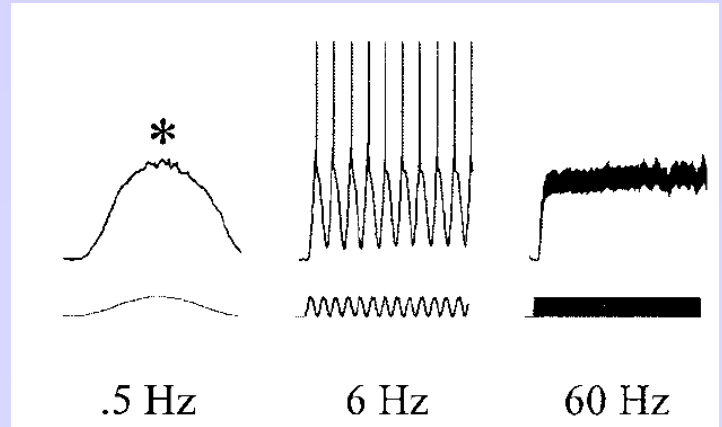


# Fano Factor

- Allows for the uncovering of frequency/time scale preferences



Entrainment  
Resonant frequency →

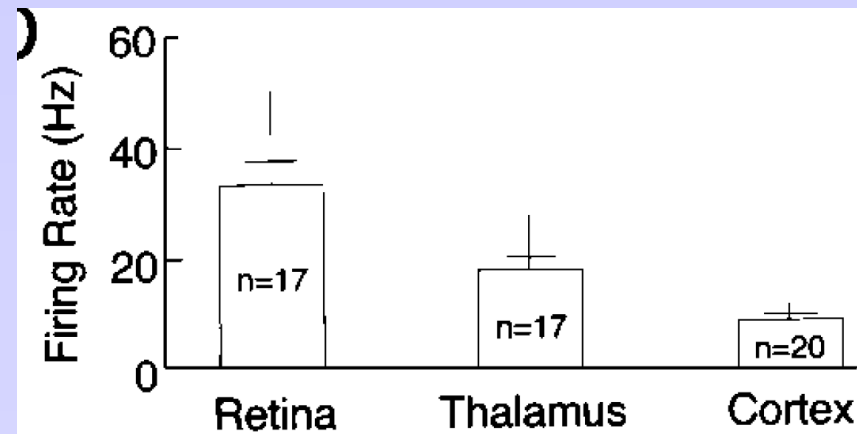
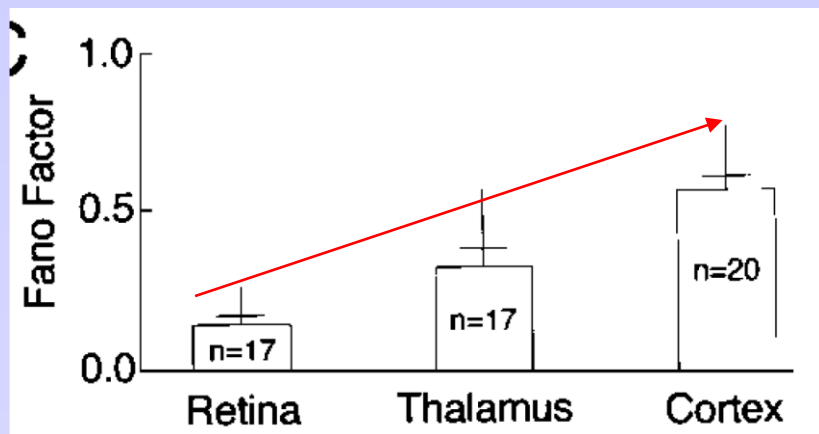


(Fellous et al. 2001)

# Fano Factor

- Measuring the variability of neural responses to the same stimuli, **across multiple brain areas**

Simultaneous recordings in anesthetized cat: retina, LGN, V1



(Kara et al. 2000)

➔ Activity is less and less regular from sensation to perception

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# Homework 2 – due Next week

- Q1: Using the simpleneuron model: Record the membrane potential (type '*RecordMEMPOT(0)*'). Run the model for 10 seconds (spontaneous activity). Use *SaveMEMPOT()* to save the voltage values of the simulation.
  - > Compute the mean and standard deviation of the membrane potential and compare with (Pare et.al. 1998).
- Q2: Write a routine that takes a spike train and returns the firing rate, the CV and the CV2.
- Q3: Increase the level of noise of the model (in the shell, type '*neurs[0].noise.g\_e0=0.02*'). Record the action potentials of neuron 0 (type '*RecordAP(0)*'). Run the Neuron model for 150 seconds (spontaneous activity). Use *SaveAP()* to save the times of the action potentials.
  - > Compute the cumulative firing rate, CV and CV2. Plot the CV2 Vs mean ISI (see Holt et al. 1996, fig 2). What do you see?
- Q4 (optional):  
Generate 2000 spikes Poisson distributed at 20 Hz with a 4 ms absolute refractory period.
  - > Modify the spike train to produce as '**strange**' of a return map as possible. Plot the return map and a sample of the spike train. Make sure to explain the features of the map, and how they relate to the modifications you introduced.